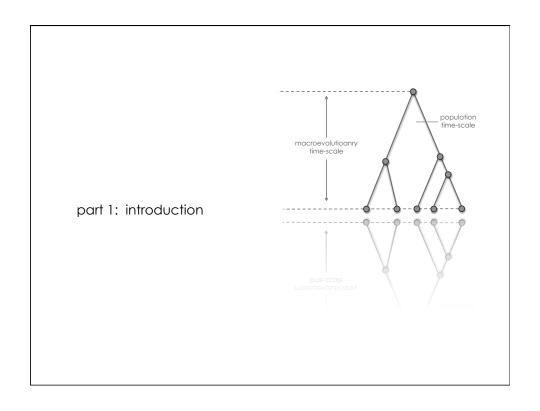
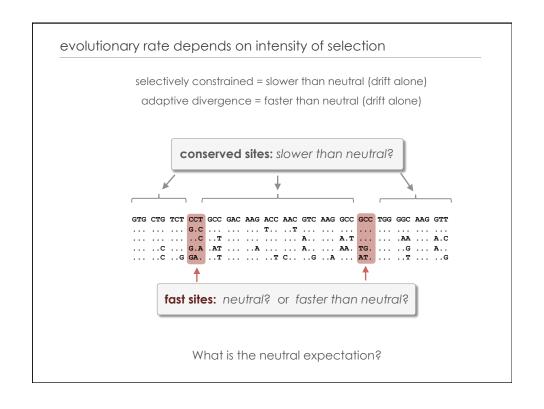
# codon substitution models and the analysis of natural selection pressure



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# The goals and the plan neutral theory dN/dS mechanistic process phenomenological outcomes part 1: introduction part 2: mechanistic process MutSel framework part 3: phenomenological freq dependent selection episodic selection modeling shifting balance types of models 3 analysis tasks phylogenomic example best practices



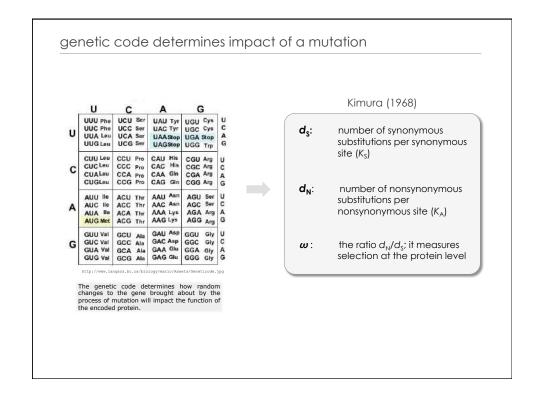


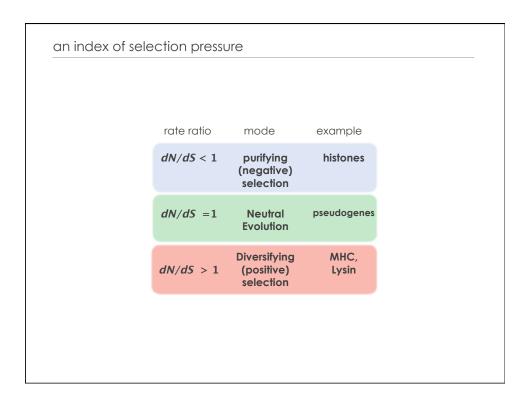
neutral theory of molecular evolution (Kimura 1968)

the number of new mutations arising in a diploid population

the fixation probability of a new mutant by drift

The substitution (fixation) rate, k  $k = 2N\mu \times 1/2N$ the elegant simplicity of neutral theory:  $k = \mu$ 





an index of selection pressure

# Why use $d_N$ and $d_S$ ? (Why not use raw counts?)

example of counts:

300 codon gene from a pair of species 5 synonymous differences

5 nonsynonymous differences

5/5 = 1

why <u>don't</u> we conclude that rates are equal (i.e., **neutral evolution)?** 

# the genetic code & mutational opportunities

Relative proportion of different types of mutations in hypothetical protein coding sequence.								
	Expected number of changes (proportion)							
Туре	All 3 Positions 1 <sup>st</sup> positions		2 <sup>nd</sup> positions	3 <sup>rd</sup> positions				
Total mutations	549 (100)	183 (100)	183 (100)	183 (100)				
Synonymous	134 (25)	8 (4)	0 (0)	126 (69)				
Nonsyonymous	392 (71)	166 (91)	176 (96)	57 (27)				
nonsense	23 (4)	9 (5)	7 (4)	7 (4)				

Modified from Li and Graur (1991). Note that we assume a hypothetical model where all codons are used equally and that all types of point mutations are equally likely.

# Why do we use $d_N$ and $d_S$ ?

same example, but using  $d_N$  and  $d_S$ :

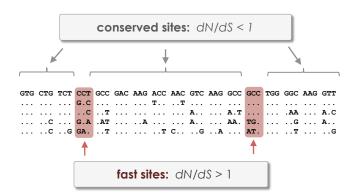
Synonymous sites = 
$$25.5\%$$
  
S =  $300 \times 3 \times 25.5\% = 229.5$ 

Nonsynonymous sites = 
$$74.5\%$$
  
N =  $300 \times 3 \times 74.5\% = 670.5$ 

So, 
$$d_S = 5/229.5 = 0.0218$$
  
 $d_N = 5/670.5 = 0.0075$ 

 $d_N/d_S(\omega) = 0.34$ , purifying selection !!!





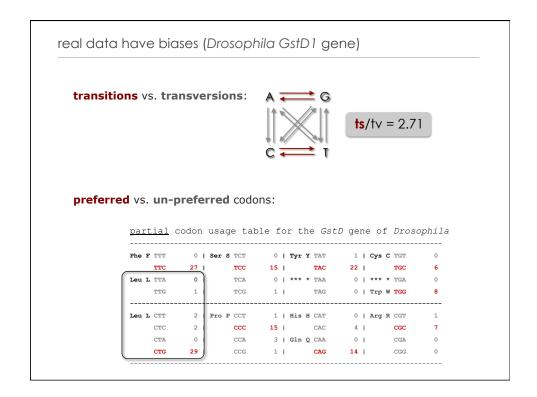
**conclusion:** *dN* differs from *dS* due to the effect of selection on the protein.

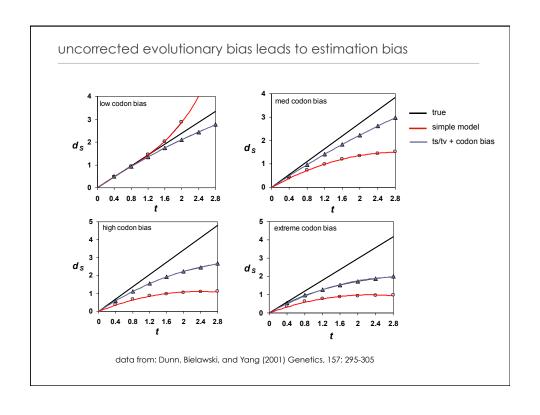
#### mutational opportunity vs. physical site

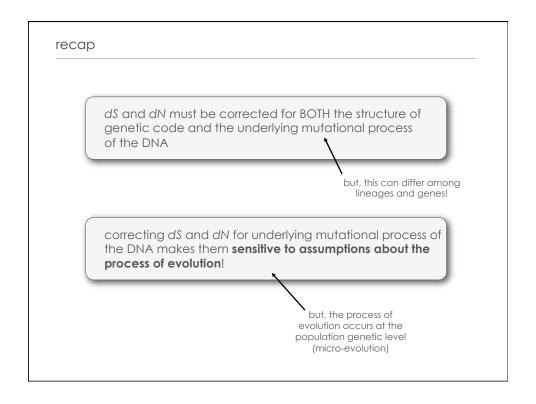
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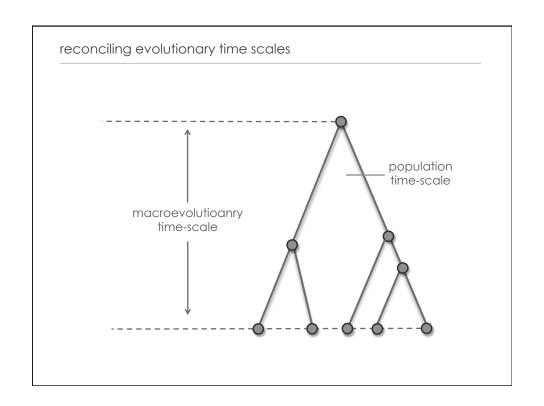
**Note** that by framing the counting of sites in this way we are using a "mutational opportunity" definition of the sites. Thus, a synonymous or non-synonymous site is <u>not</u> considered a physical entity!

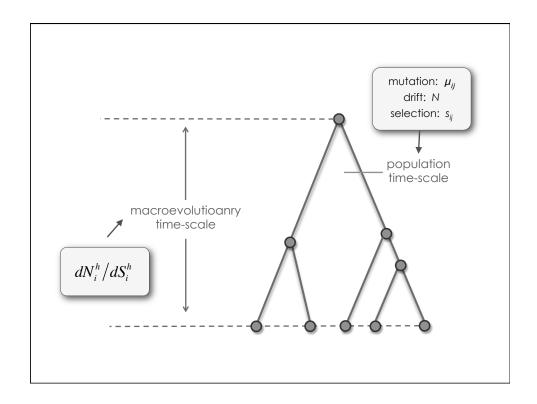
**Note** that we assume a hypothetical model where all codons are used equally and that all types of point mutations are equally likely.

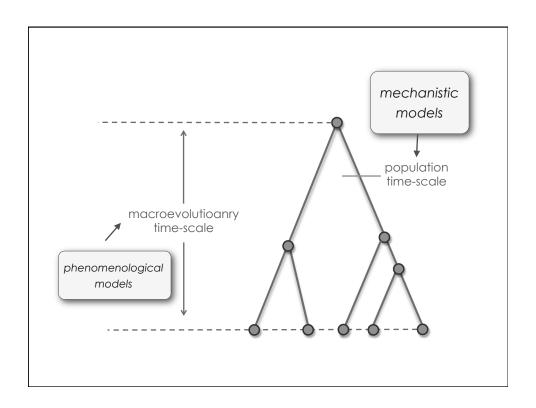


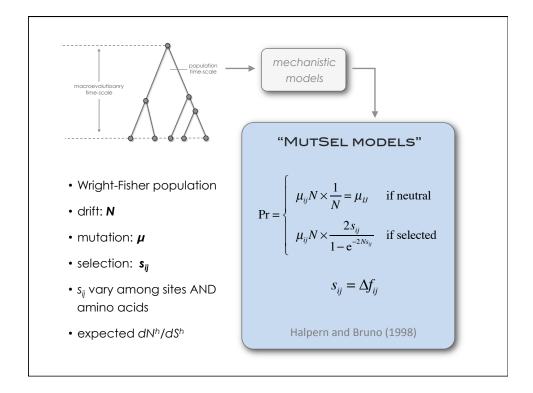








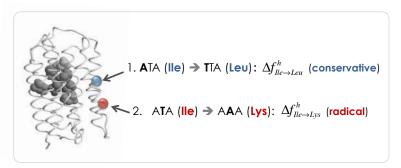




fixation probability with selection population genetics at a single codon site (h)  $f^h = \left\langle f_1 \;,\; \dots, f_{61} \right\rangle$  selection coefficients  $s^h_{ij} = f^h_j - f^h_i$  fixation probability (Kimura, 1962)  $\Pr(s^h_{ij}) = \frac{2s^h_{ij}}{1-\mathrm{e}^{-2Ns^h_{ij}}}$ 

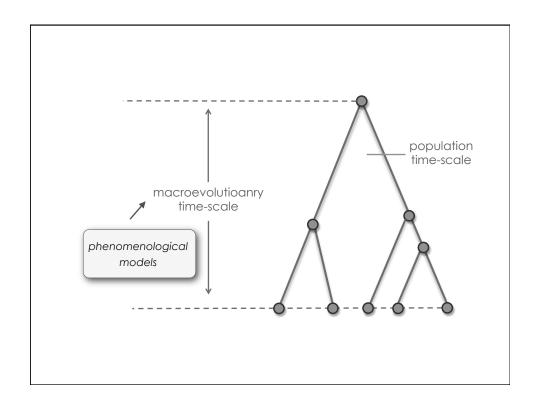
# fixation probability with selection

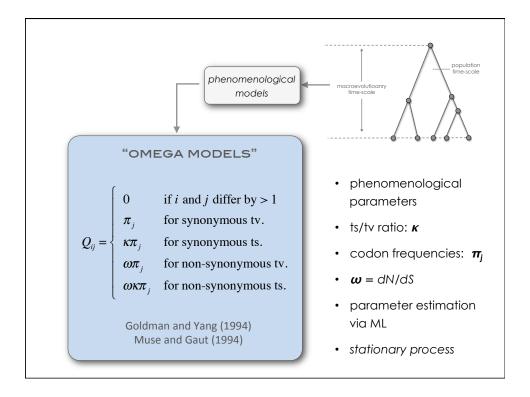
**MutSel:** selection favours amino acids with higher fitness (if N is large enough)



**realism**: fitness expected to differ among sites and amino acids according to protein function

the cost of realism: too complex to fit such a model to real data





the instantaneous rate matrix, Q, is very big: 61 × 61

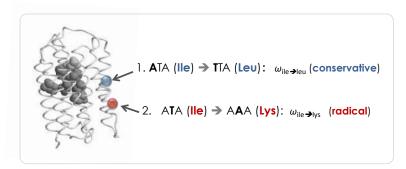
phenomenological codon models: just a few parameters are needed to cover the 3721 transitions between codons!

	to codon below:							
From codon below:	TTT (Phe)	TTC (Phe)	TTA (Leu)	TTG (Leu)	CTT (Leu)	CTC (Leu)	•••▶	GGG (Gly)
TTT (Phe)		$\kappa\pi_{\mathrm{TTC}}$	$\omega\pi_{\mathrm{TTA}}$	$\omega\pi_{\mathrm{TTG}}$	ωκπ <sub>TTT</sub>	0	•••	0
TTC (Phe)	$\kappa\pi_{\mathrm{TTT}}$		$\omega\pi_{\mathrm{TTA}}$	$\omega\pi_{\mathrm{TTG}}$	0	$\omega \kappa \pi_{\mathrm{CTC}}$	•••	0
TTA (Leu)	$\omega\pi_{\mathrm{TTT}}$	$\omega\pi_{\mathrm{TTC}}$			0	0	…▶	0
TTG (Leu)	$\omega\pi_{\mathrm{TTT}}$	$\omega\pi_{\mathrm{TTC}}$	$\kappa\pi_{\mathrm{TTA}}$		0	0	***	0
CTT (Leu)	$\omega \kappa \pi_{\mathrm{TTT}}$	0	0	0		$\kappa\pi_{\mathrm{CTC}}$	•••	0
CTC (Leu)	0	$\omega \kappa \pi_{\mathrm{TTC}}$	0	0	$\kappa\pi_{\mathrm{TTT}}$		***	0
<b>:</b> ▼	: *	ŧ	<u>:</u>	<u>:</u>	÷	<u>:</u>	**************************************	
GGG (Gly)	0	0	0	0	0	0	0	

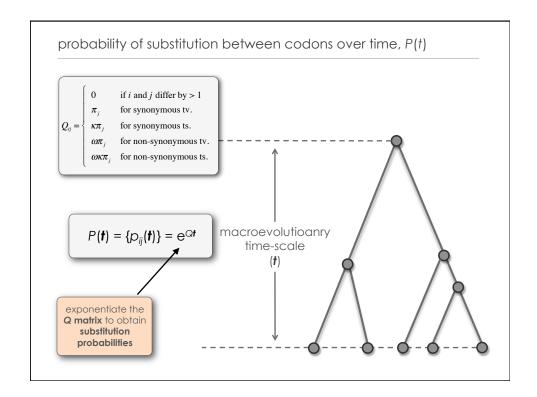
<sup>\*</sup> This is equivalent to the codon model of Goldman and Yang (1994). Parameter  $\omega$  is the ratio  $d_{\rm N}/d_{\rm S}$ ,  $\kappa$  is the transition/transversion rate ratio, and  $\pi_i$  is the equilibrium frequency of the target codon (i).

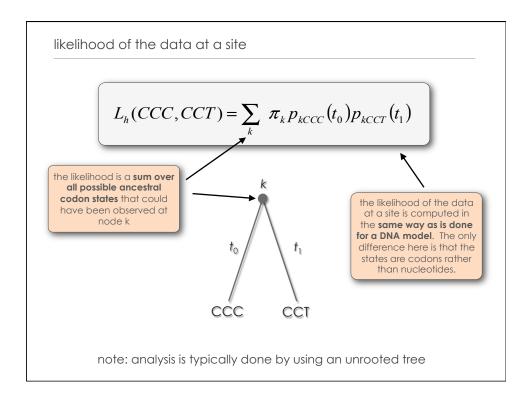
# substitution probability with selection

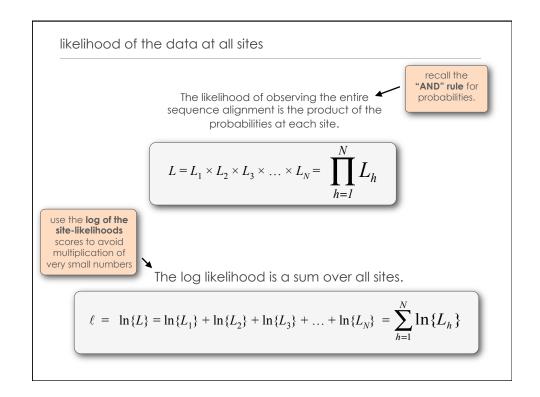
**intentional simplification**: all amino acid substitutions have the same  $\boldsymbol{\omega}!$ 



**contradiction?** selection should favour amino acids with higher fitness.



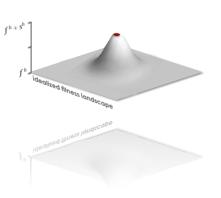




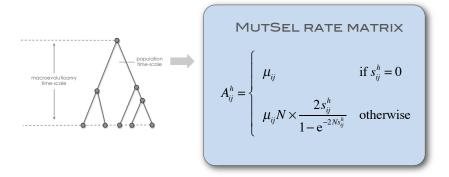
#### summary

- dN/dS is a measure of selection pressure that can be connected to a mechanistic process of population genetic evolution (MutSel models)
- dN/dS can be estimated from multi-sequence alignments as a parameter ( $\omega$ ) in a phenomenological model of sequence evolution
- estimates of dN/dS for real data must be corrected for the underlying process of evolution for those data
- estimates of dN/dS can be sensitive to assumptions about the underlying process of evolution
- phenomenological estimates of dN/dS are highly simplistic summaries of a much more complex evolutionary process

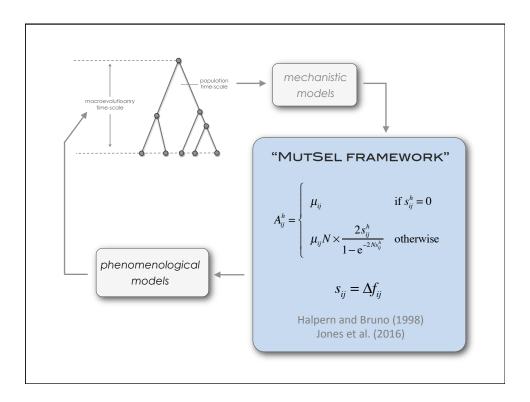
part 2: mechanistic processes of codon evolution



### site-specific MutSel rate matrix



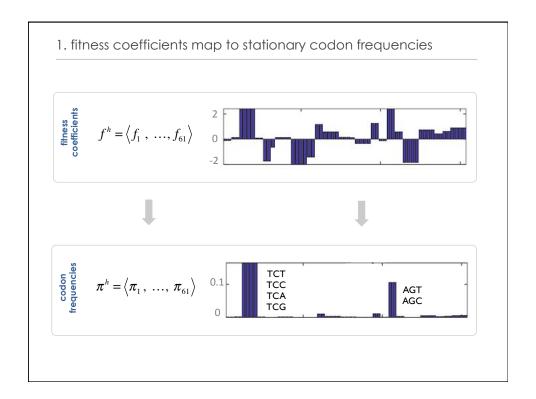
- MutSel time-scale is infinitesimal compared to substitution scale
- MutSel probabilities approximate the instantaneous site-specific rate matrix, A
- $\mu_{ij}$  = nucleotide GTR process (before the effect of selection)



site-specific MutSel rate matrix

two explicit ways to reconcile **population genetics** and **macroevolution**:

- 1. map fitness to equilibrium frequencies
- 2. macroevolution index of selection intensity



#### 2. from fitness coefficients to dN/dS

#### MUTSEL RATE MATRIX

$$dN^{h} / dS^{h} = \frac{E[\text{evolution w/ selection}]}{E[\text{drift away from equilibrium set by selection}]}$$

$$dN^h / dS^h = \frac{\sum_{i \neq j} \pi_i^h A_{ij}^h I_N}{\sum_{i \neq j} \pi_i^h \mu_{ij} I_N}$$

- $dN/dS = \omega$  when matrix  $A^h$  is replaced by matrix Q of model M0
- dN/dS is an analog of  $\omega$  under MutSel

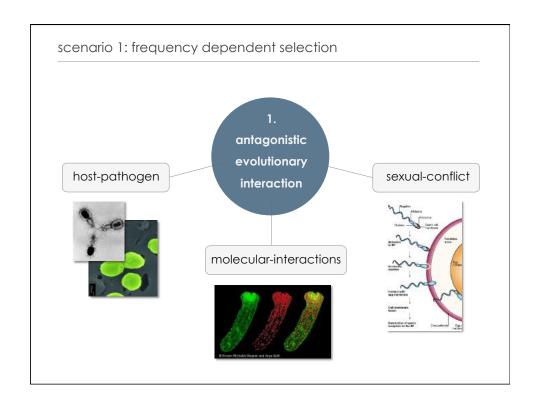
positive selection: 3 evolutionary scenarios

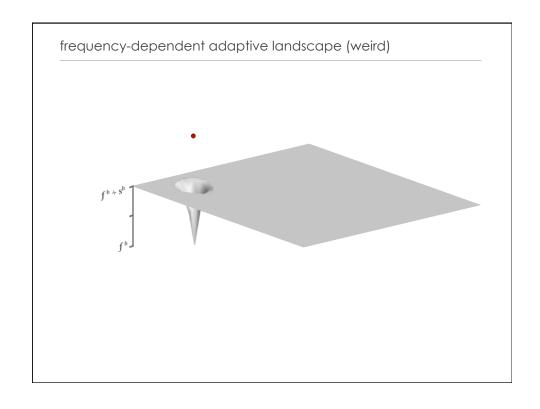
- frequency dependent selection
- 2 episodic adaptation

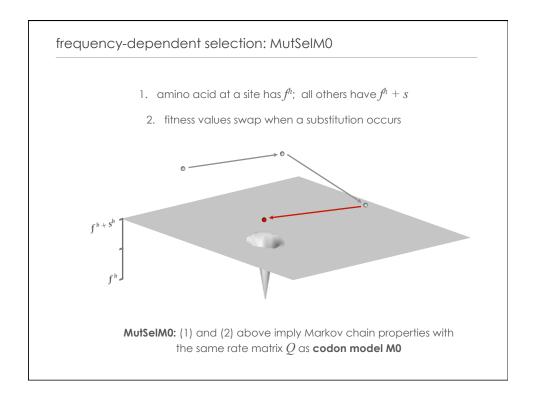
3 shifting balance

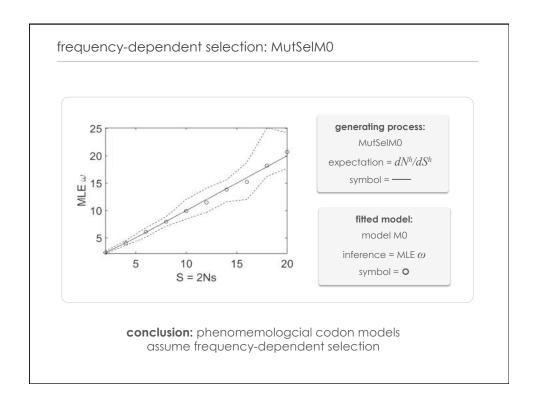
dynamic fitness landscape

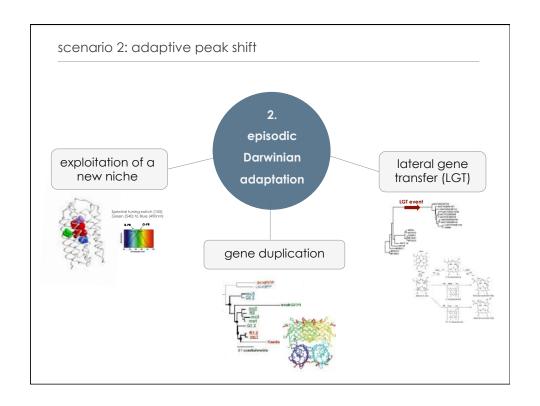
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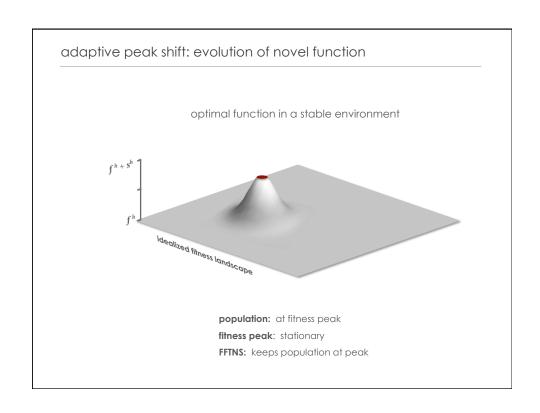


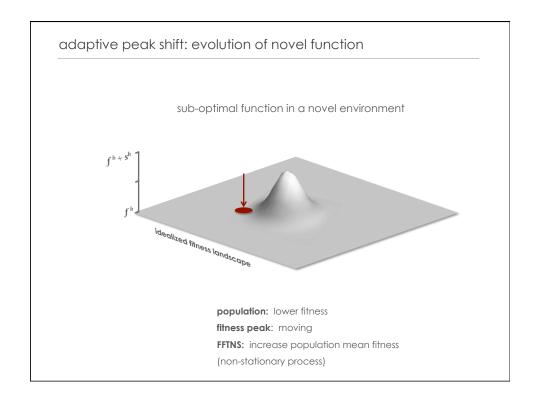


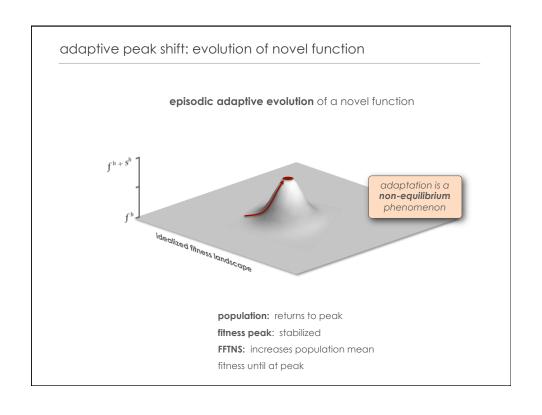












# adaptive peak shift: MutSelES model

### BIOLOGY LETTERS

#### rsbl.royalsocietypublishing.org

## Research



Gite this article: dos Reis M. 2015 How to calculate the non-synonymous to synonymous rate ratio of protein-coding genes under the Fisher – Wright mutation – selection framework. Biol. Lett. 11: 20141031. http://dx.do.org/10.1098/rsbl.2014.1031

Received: 8 December 2014 Accepted: 16 March 2015

#### Molecular evolution

How to calculate the non-synonymous to synonymous rate ratio of protein-coding genes under the Fisher – Wright mutation – selection framework

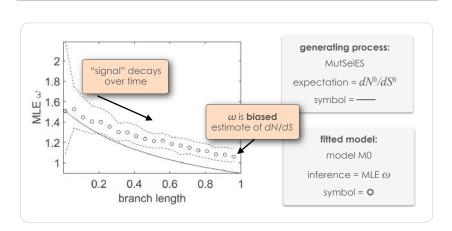
#### Mario dos Reis

Department of Genetics, Evolution and Environment, University College London, Gower Street, London WCIE 6BT, UK

First principles of population genetics are used to obtain formulae relating the non-synonymous to synonymous substitution rate ratio to the selection coefficients acting at codon sites in protein-coding genes. Two theoretical cases are discussed and two examples from real data (a chloroplast gene and a virus polymerase) are given. The formulae give much insight into the dynamics of non-synonymous substitutions and may inform the development of methods to detect adaptive evolution.

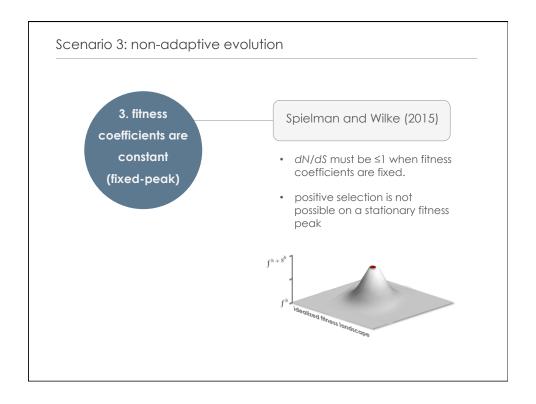
4. The non-synonymous rate during adaptive evolution

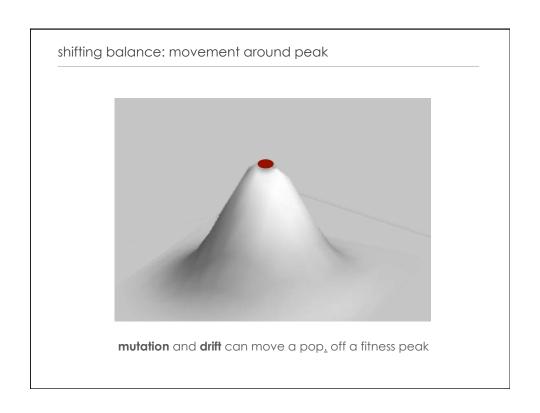
## adaptive peak shift: MutSelES

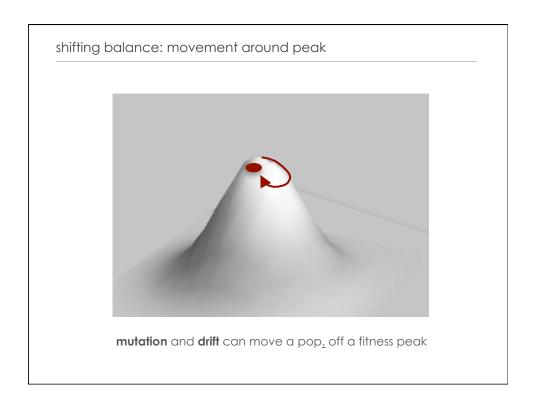


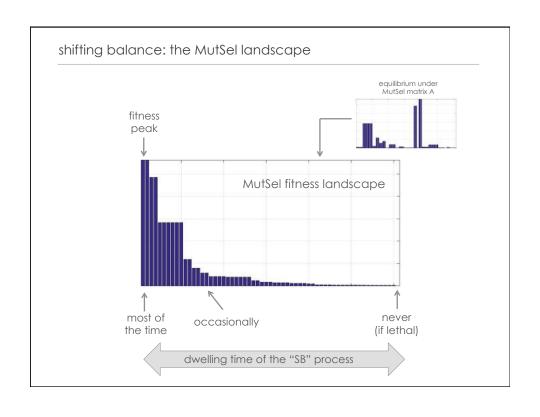
**conclusion :** episodic models "work" because w>1 is a consequence of a system moving towards a new fitness peak.

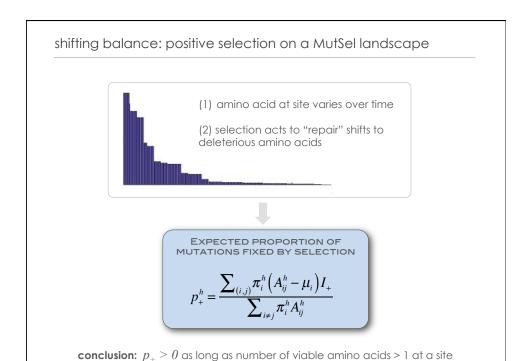
**conclusion :** episodic models "work" because they are sensitive to non-stationary behavior

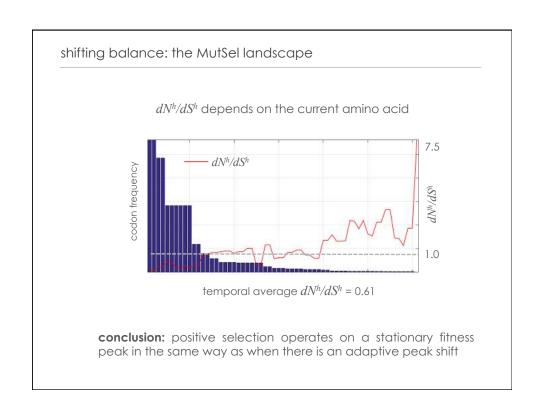


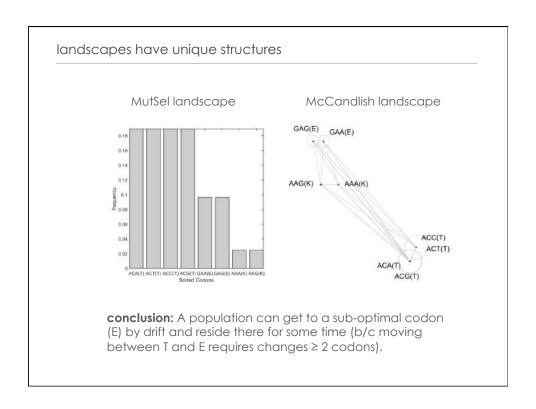


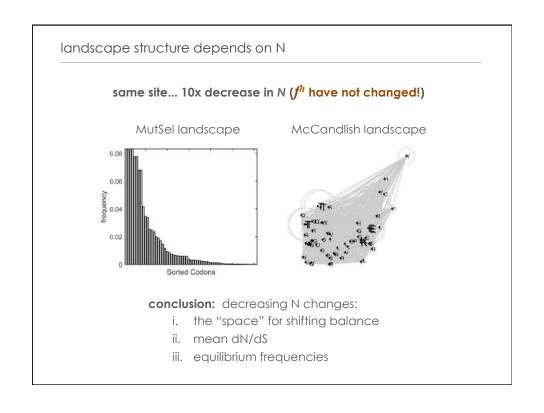


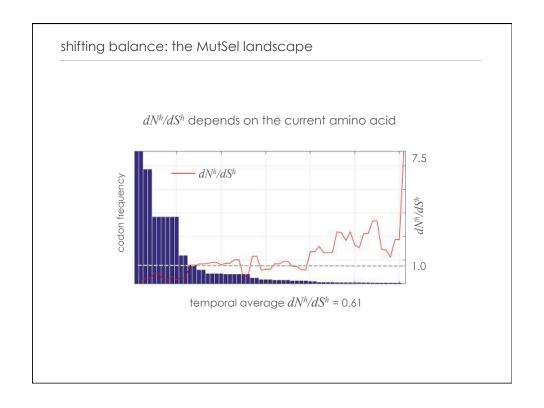


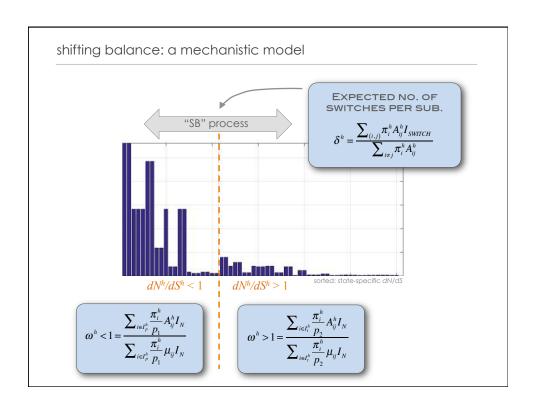


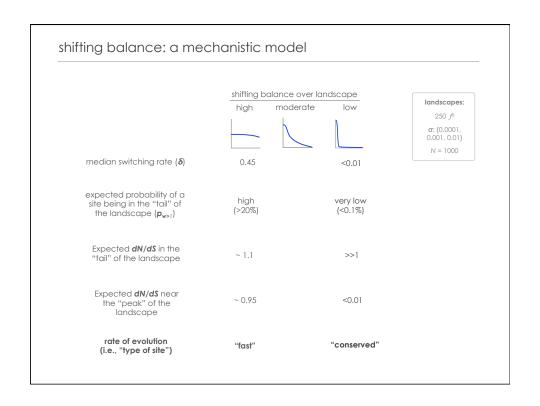


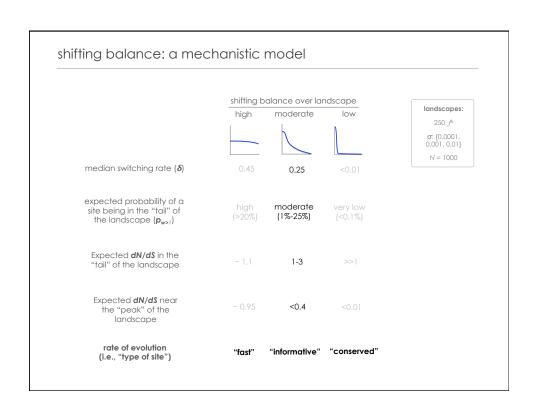












#### gene sequences

human cow rabbit rat opossum

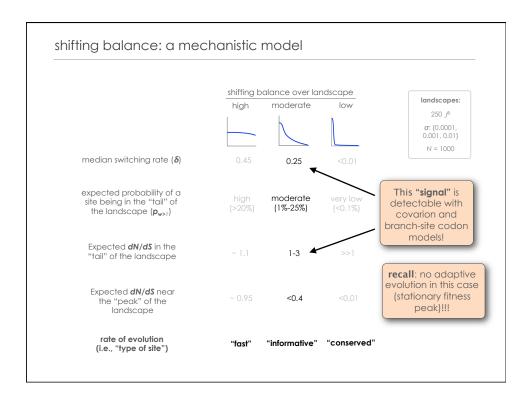
#### covarion-like model of evolution

2 selective regimes (low & high): sites CAN switch regime



— Low  $(\omega_1)$  — HIGH  $(\omega_2)$  proportion of  $\omega_1$  sites:  $\rho_1$  proportion of  $\omega_2$  sites:  $\rho_2$  switching:  $\delta$ 

the covarion-like codon model can be fit to real data (Guindon et al., 2004)



#### summary

- standard codon models (single  $\omega$ ) assume frequency dependent selection, which yields a persistent dN/dS > 1
- episodic adaptive evolution leads to transient dN/dS > 1
- phenomenological codon models assume a stationary evolutionary process; adaptive evolution is non-stationary
- estimates of  $\pmb{\omega}$  for episodic adaptive evolution are upwardly biased because adaptive evolution is non-stationary
- protein evolution on a static fitness landscape has temporal dynamics that include positive selection
- MutSel landscapes can be complex and a site can reside at a suboptimal state for extended periods of time
- rate variation among sites reflects the interplay between mutation, drift, and selection (i.e., shifting balance dynamics)