

# Analysis of (bulk) RNAseq data

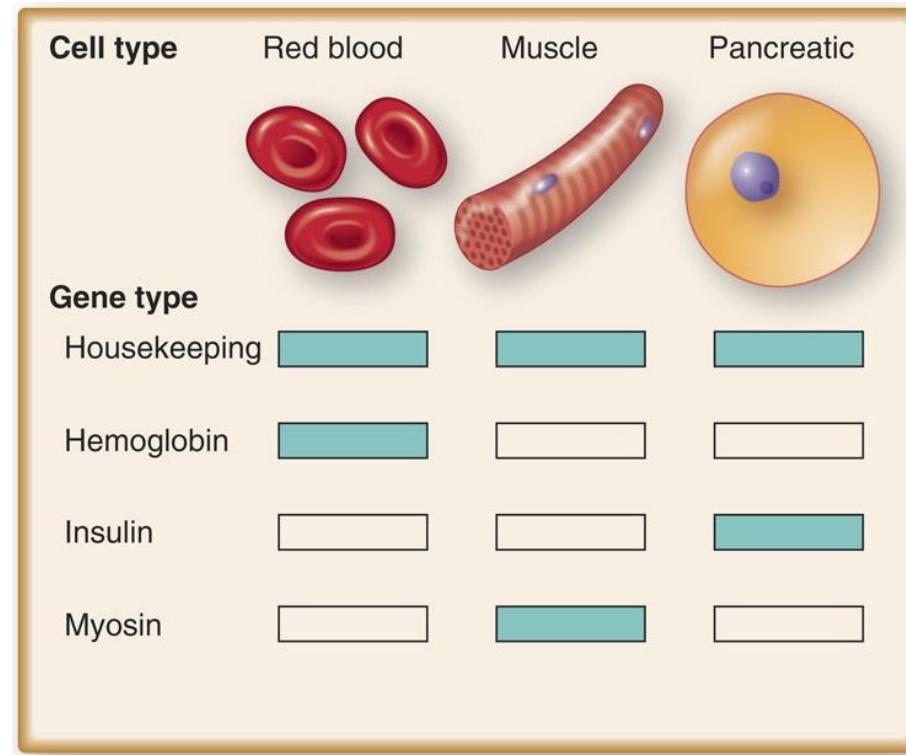
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Researcher  
Lund University

**Česky Krumlov**  
21-01-2026

# Gene expression

The selective activity of certain genes is a highly regulated process

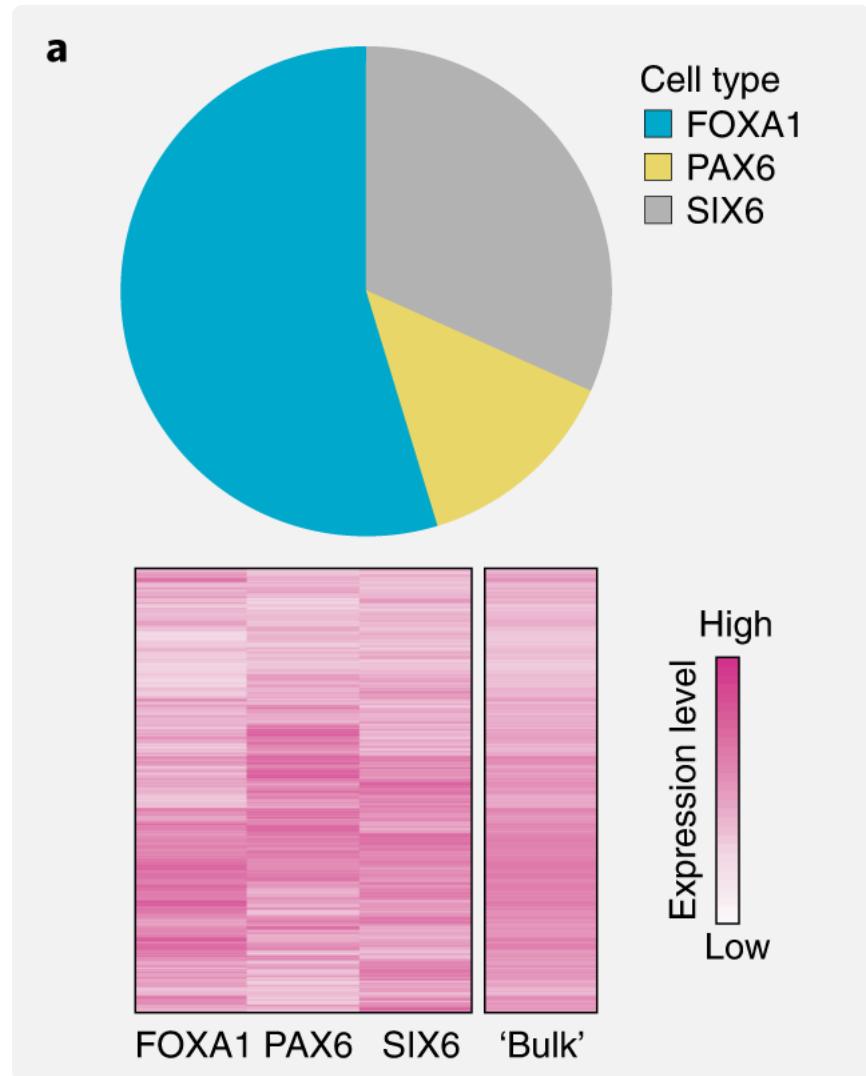
Gene expression is a characteristic of space (e.g., cell type, tissue, etc.) and time (e.g., developmental stage, time after event)



# Gene expression

The selective activity of certain genes is a highly regulated process

**Gene expression is a characteristic of space (e.g., cell type, tissue, etc.) and time (e.g., developmental stage, time after event)**



Price et al. 2022. Nature Ecology and Evolution

# What are some questions we can answer with bulk RNAseq data?

How many genes are being expressed?

Which genes are uniquely expressed?

Are patterns of gene expression different among samples?

Are patterns of expression different among genes?

Does gene expression differ between groups? According to a certain variable?

Which genes are co-expressed?

What are the functional roles of groups of differently expressed genes?

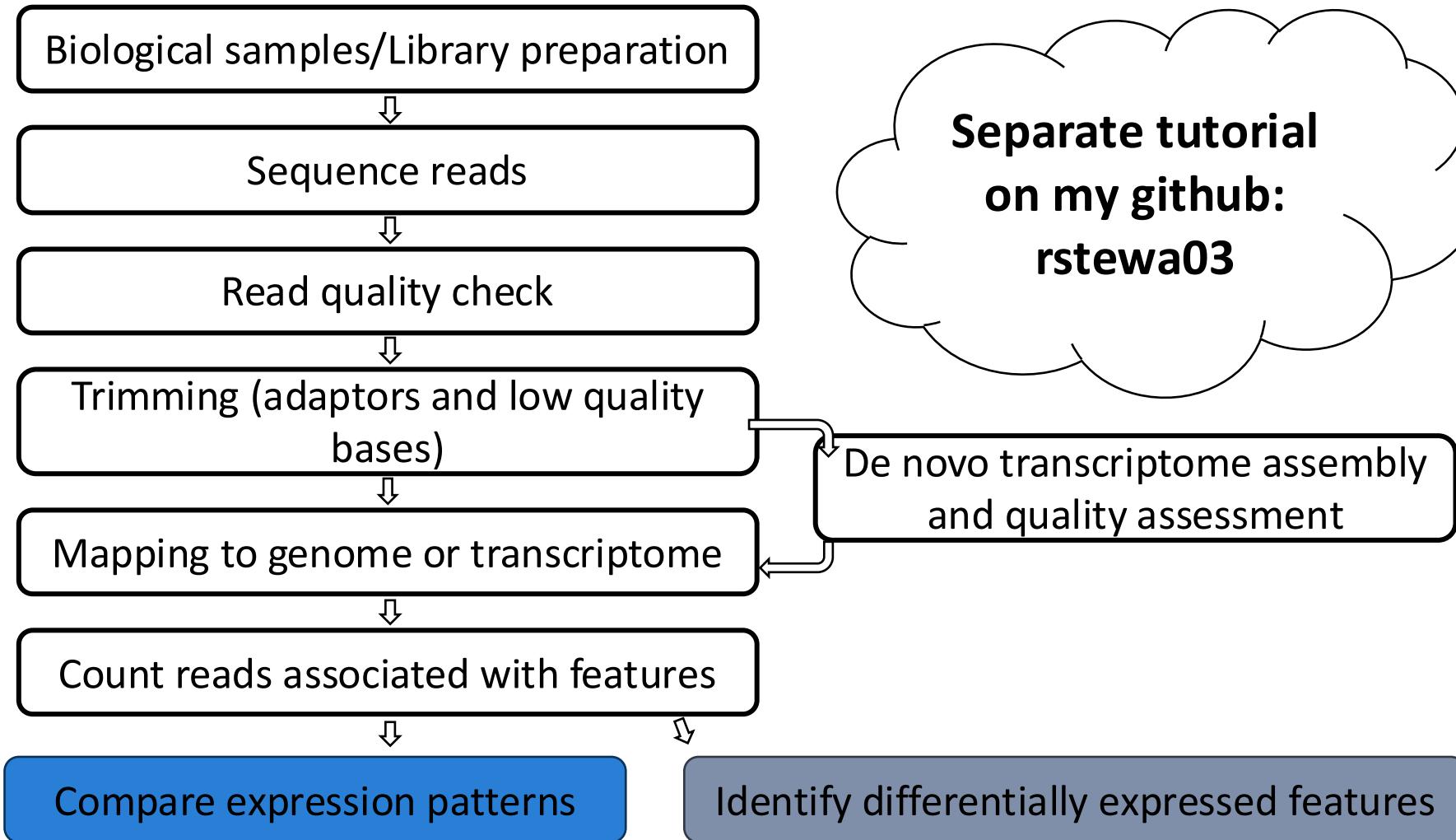
# Lab activities

- **Part 1** Exploring patterns in RNAseq data
- **Part 2** Differential gene expression analysis
- **Part 3** Functional enrichment of gene sets

## Structure:

- Short background
- Open work time
- Review

# Gene expression analysis



# Quality control

## Reads: To trim or not to trim?

- genome annotation, variant calling, transcriptome assembly : Trim!
- Anything else, maybe trim lightly?
  - adapters + low quality score (Q10-15)

## Reference genome considerations:

- What maps where:
  - Recent duplications?
  - Highly repetitive content?
  - Missing content?

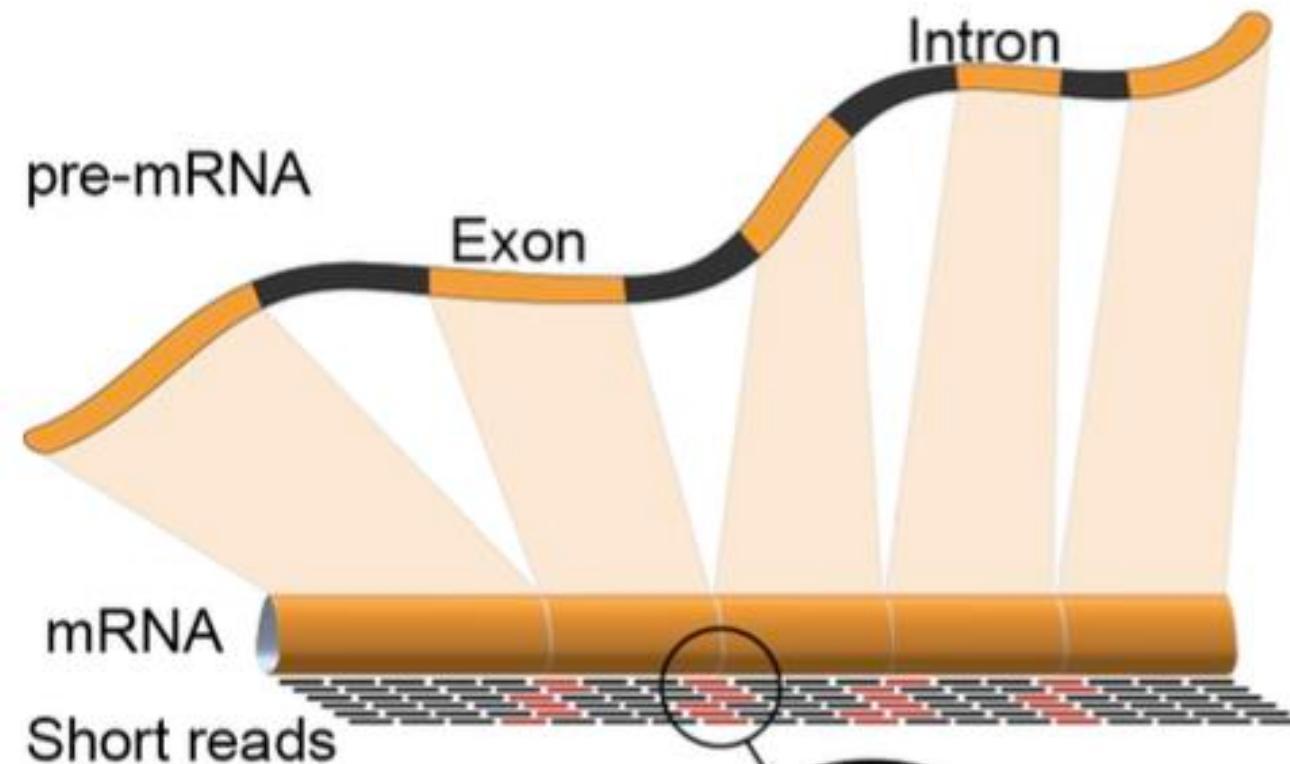
## Annotation considerations:

- What features have been annotated?
- Was RNAseq data used in the annotation?
  - *What RNA? Life stage? Sex?*

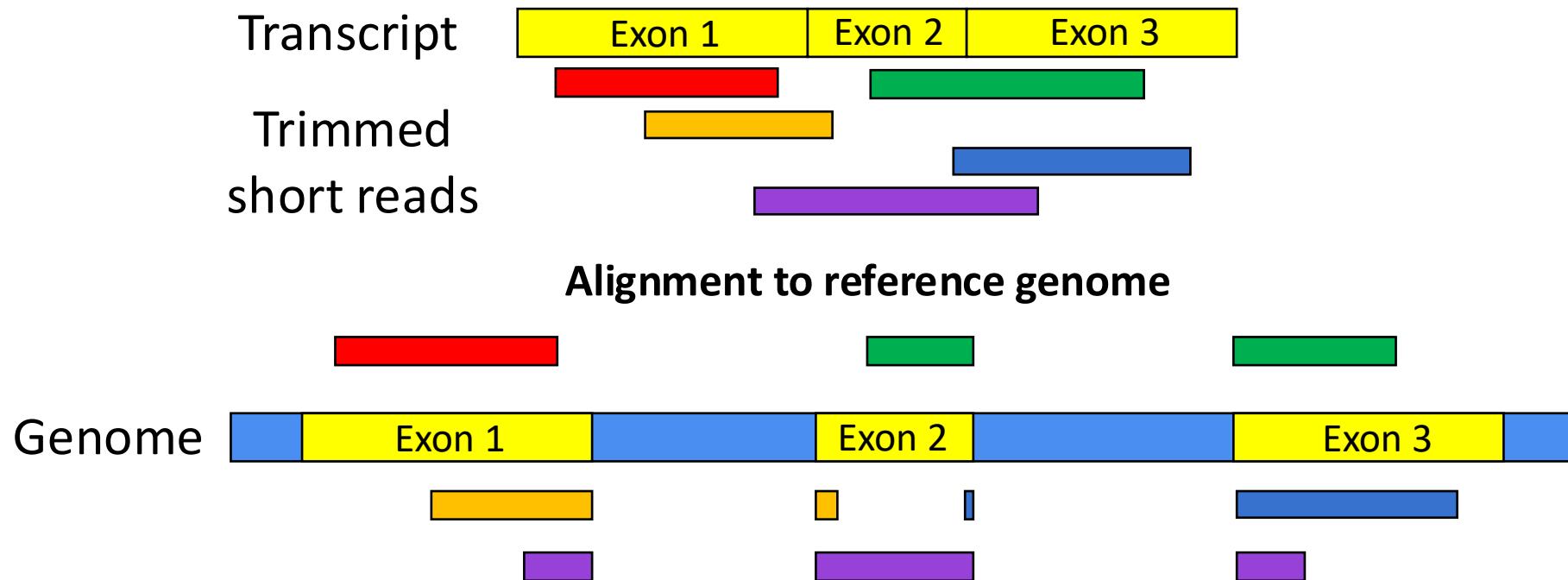
Williams et al. 2016 BMC Bioinformatics,  
Liao and Shi 2020 NAR Genomics and Bioinformatics

# RNA sequence alignment to a reference

What are some challenges when aligning RNA-seq reads to the reference genome?



# Splice-aware sequence alignment

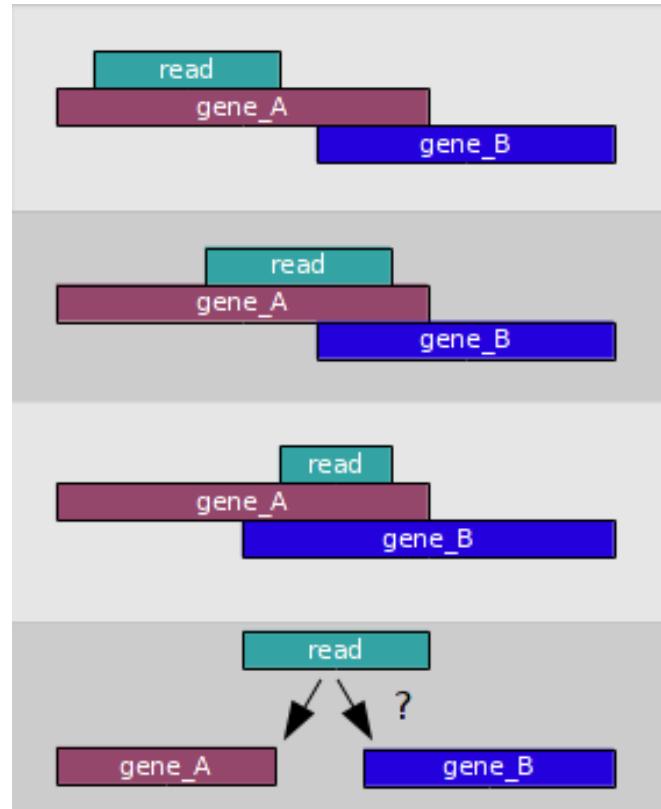
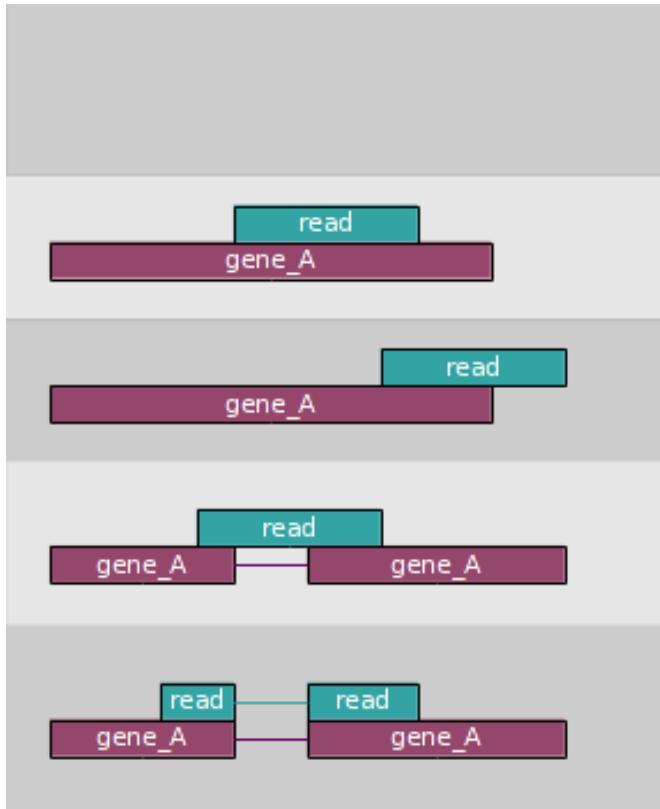


# Counting reads as a measure of expression

- Two common counting tools are **featureCounts** and **htseq**.
- Total read count associated with a gene (meta-feature)
  - sum of reads mapping to exons (features) that are a part of that gene.
- Alternative approach: pseudoalignment and quantification of transcripts like **Salmon** and **Kallisto**

```
genomics@ip-172-31-11-182:[~/workshop_materials/differential_expression/refs]$ head Pca_annotation.gtf
LG1  AUGUSTUS transcript 22193 24413 . - . transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1  AUGUSTUS exon 22193 22320 . - . transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1  AUGUSTUS exon 23838 24048 . - . transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1  AUGUSTUS exon 24390 24413 . - . transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1  AUGUSTUS CDS 22193 22320 . - 2 transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1  AUGUSTUS CDS 23838 24048 . - 0 transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1  AUGUSTUS CDS 24390 24413 . - 0 transcript_id "Polcal_g1.t1"; gene_id "Polcal_g1";
LG1  AUGUSTUS transcript 79912 80136 . - . transcript_id "Polcal_g2.t1"; gene_id "Polcal_g2";
LG1  AUGUSTUS exon 79912 80136 . - . transcript_id "Polcal_g2.t1"; gene_id "Polcal_g2";
LG1  AUGUSTUS CDS 79912 80136 . - 0 transcript_id "Polcal_g2.t1"; gene_id "Polcal_g2";
genomics@ip-172-31-11-182:[~/workshop_materials/differential_expression/refs]$
```

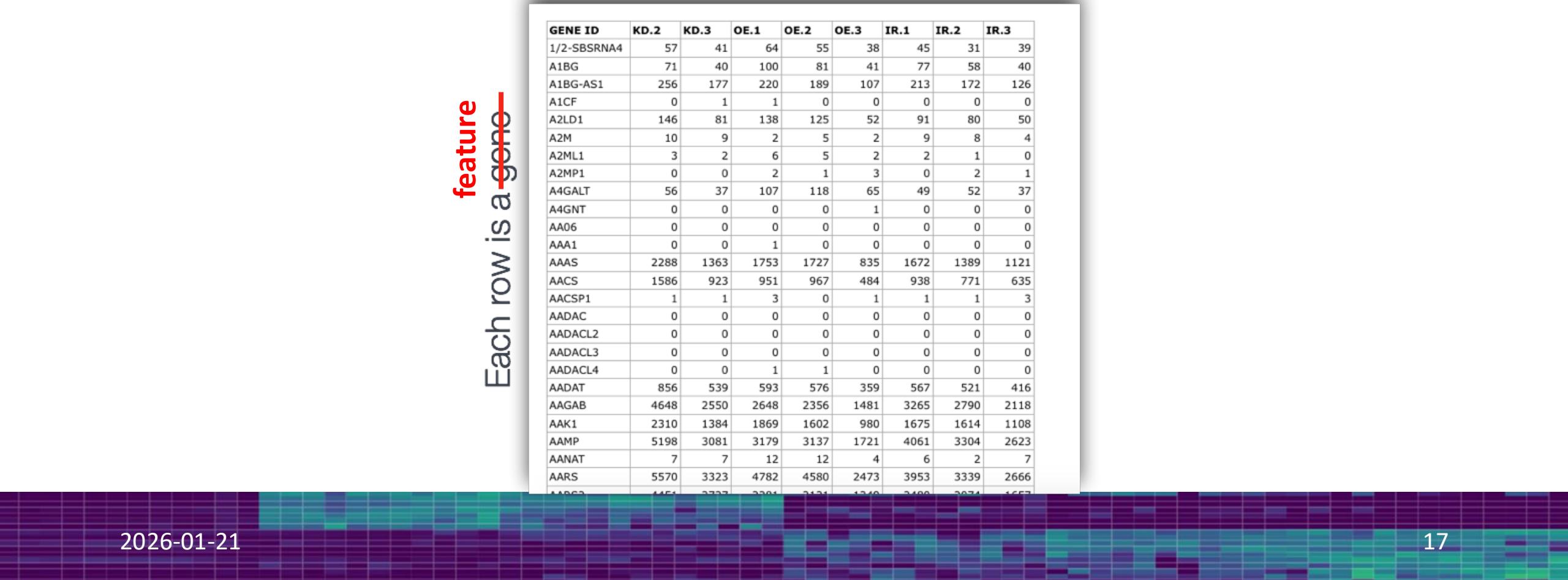
# What should count??



HTSeq manual

# Read count matrix

- Output of counting = A count matrix, with features as rows and samples as columns      Each column is a sample



GENE ID	KD.2	KD.3	OE.1	OE.2	OE.3	IR.1	IR.2	IR.3
1/2-SBSRNA4	57	41	64	55	38	45	31	39
A1BG	71	40	100	81	41	77	58	40
A1BG-AS1	256	177	220	189	107	213	172	126
A1CF	0	1	1	0	0	0	0	0
A2LD1	146	81	138	125	52	91	80	50
A2M	10	9	2	5	2	9	8	4
A2ML1	3	2	6	5	2	2	1	0
A2MP1	0	0	2	1	3	0	2	1
A4GALT	56	37	107	118	65	49	52	37
A4GNT	0	0	0	0	1	0	0	0
AA06	0	0	0	0	0	0	0	0
AAA1	0	0	1	0	0	0	0	0
AAAS	2288	1363	1753	1727	835	1672	1389	1121
AACS	1586	923	951	967	484	938	771	635
AACSP1	1	1	3	0	1	1	1	3
AADAC	0	0	0	0	0	0	0	0
AADACL2	0	0	0	0	0	0	0	0
AADACL3	0	0	0	0	0	0	0	0
AADACL4	0	0	1	1	0	0	0	0
AADAT	856	539	593	576	359	567	521	416
AAGAB	4648	2550	2648	2356	1481	3265	2790	2118
AAK1	2310	1384	1869	1602	980	1675	1614	1108
AAMP	5198	3081	3179	3137	1721	4061	3304	2623
AANAT	7	7	12	12	4	6	2	7
AARS	5570	3323	4782	4580	2473	3953	3339	2666
AARS2	4451	2727	2291	2121	1240	2480	2074	1657

# Some problems with raw counts...

- Some samples consistently have more reads, some have fewer:  
**systematic biases**

Each column is a sample

2026-01-21

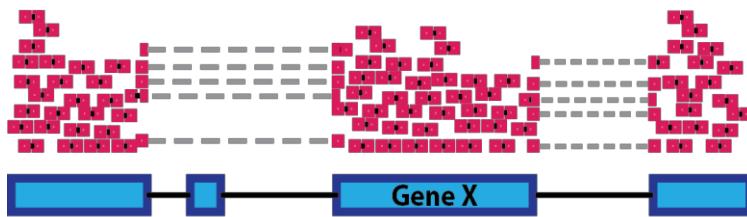
# Solution: normalization

- Normalization is NOT fitting a normal distribution or transforming data.
- Normalization aims to identify and account for the nature and magnitude of **systematic biases**
- The main factors often considered during normalization:
  - Sequencing depth (aka library size)
  - RNA composition
  - Gene length (some methods)

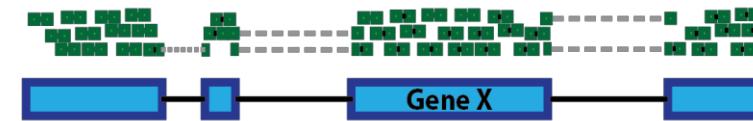
# Normalization

## Sequencing depth

Sample A Reads



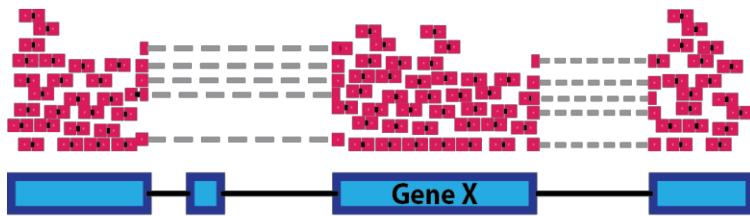
Sample B Reads



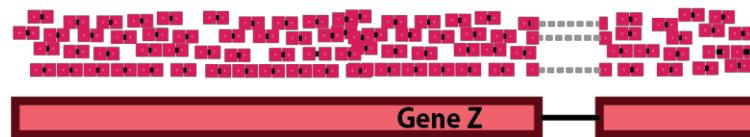
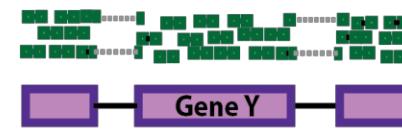
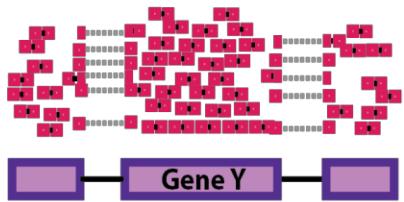
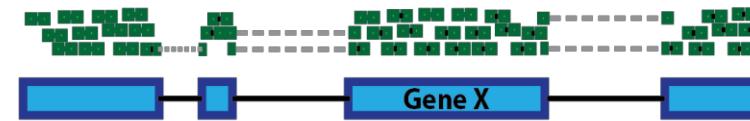
# Normalization

## Sequencing depth

Sample A Reads



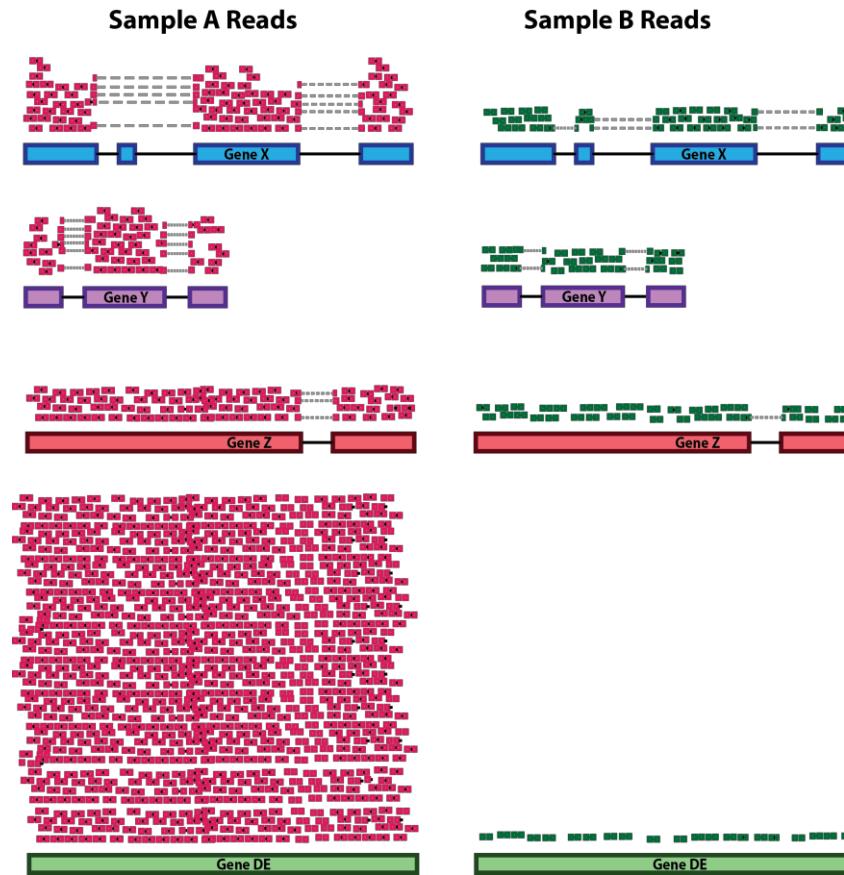
Sample B Reads



# Normalization

## RNA composition

- A few highly differentially expressed genes
- Can skew some normalization methods



# Median of ratios (MRN) normalization

- Used by DESeq2 (DGE analysis tool we will use today)
- Generates a **size factor** (also called scaling factor) for each sample to account for variation in library size

Gene	sampleA	sampleB
EF2A	1489	906
ABCD1	22	13
...	...	...

Normalized counts

Gene	sampleA	sampleB
EF2A	$1489/1.3 = 1145.39$	$906/0.77 = 1176.62$
ABCD1	$22/1.3 = 16.92$	$13/0.77 = 16.88$
...	...	...

Normalized counts are not whole numbers!

# Why don't we normalize by gene length?

- Most of the time we are comparing **WITHIN** gene, **ACROSS** samples
  - Dividing by the gene length is superfluous
  - Common tools like edgeR, limma, Deseq2
- Some metrics facilitate comparison **ACROSS** genes, **WITHIN** sample
  - These should be length-normalized
  - TPM (Transcripts Per Kilobase Million): normalize by length, then by depth
  - RPKM (Reads Per Kilobase Million): normalize by depth, then by length

# Exploring patterns in RNAseq data

## Clustering of samples

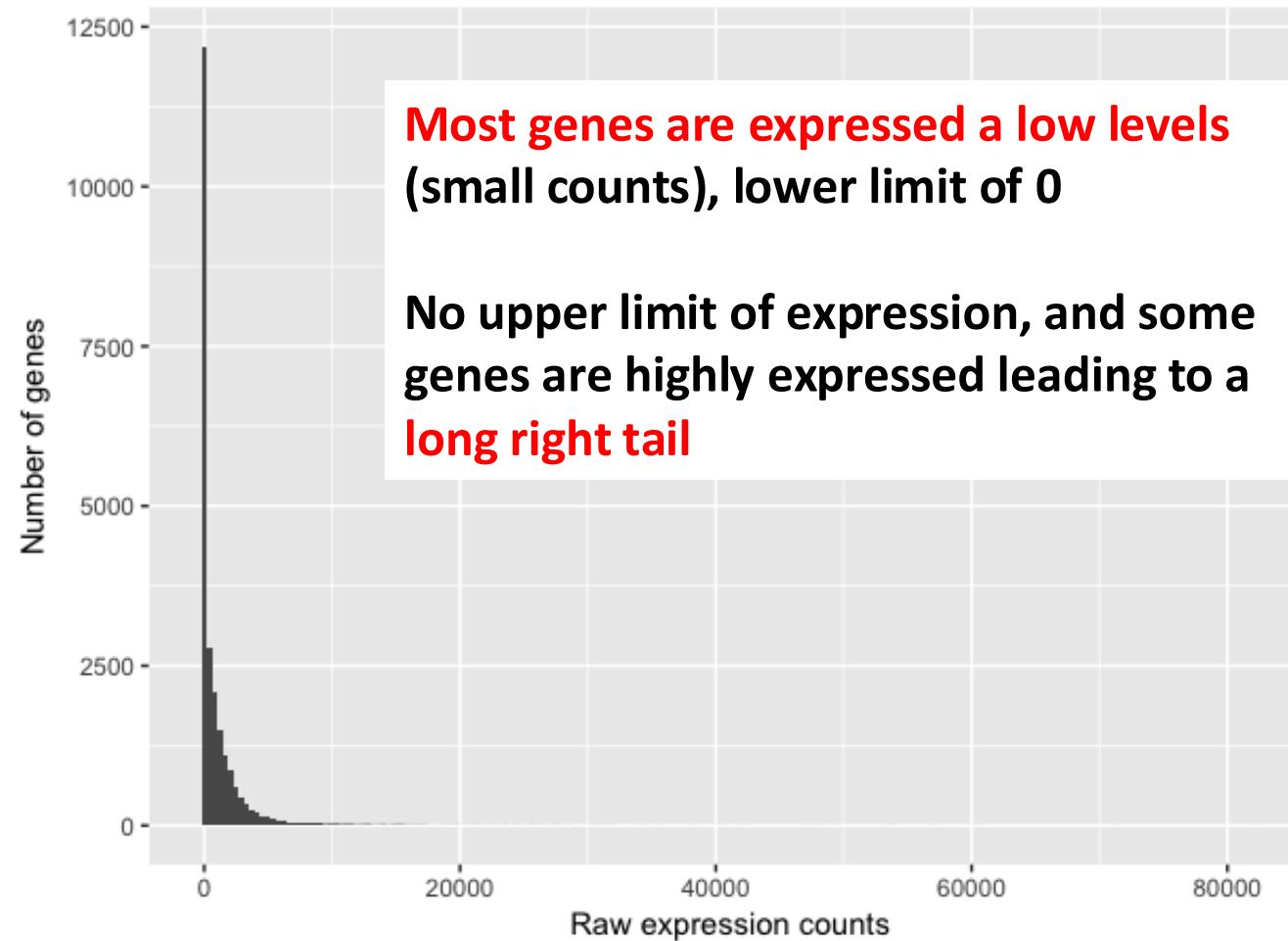
- Dimension reduction analysis (e.g., PCA, PLS, MDS)
- Clustering (e.g., hierarchical clustering, k-means clustering)

## Clustering of features

- Same as above, just focusing on features
- Weighted co-expression analysis (WGCNA, correlation among features)

# Properties of RNA-seq count data

The distribution of RNA-seq counts for a single sample:



# Data transformations for clustering and visualization

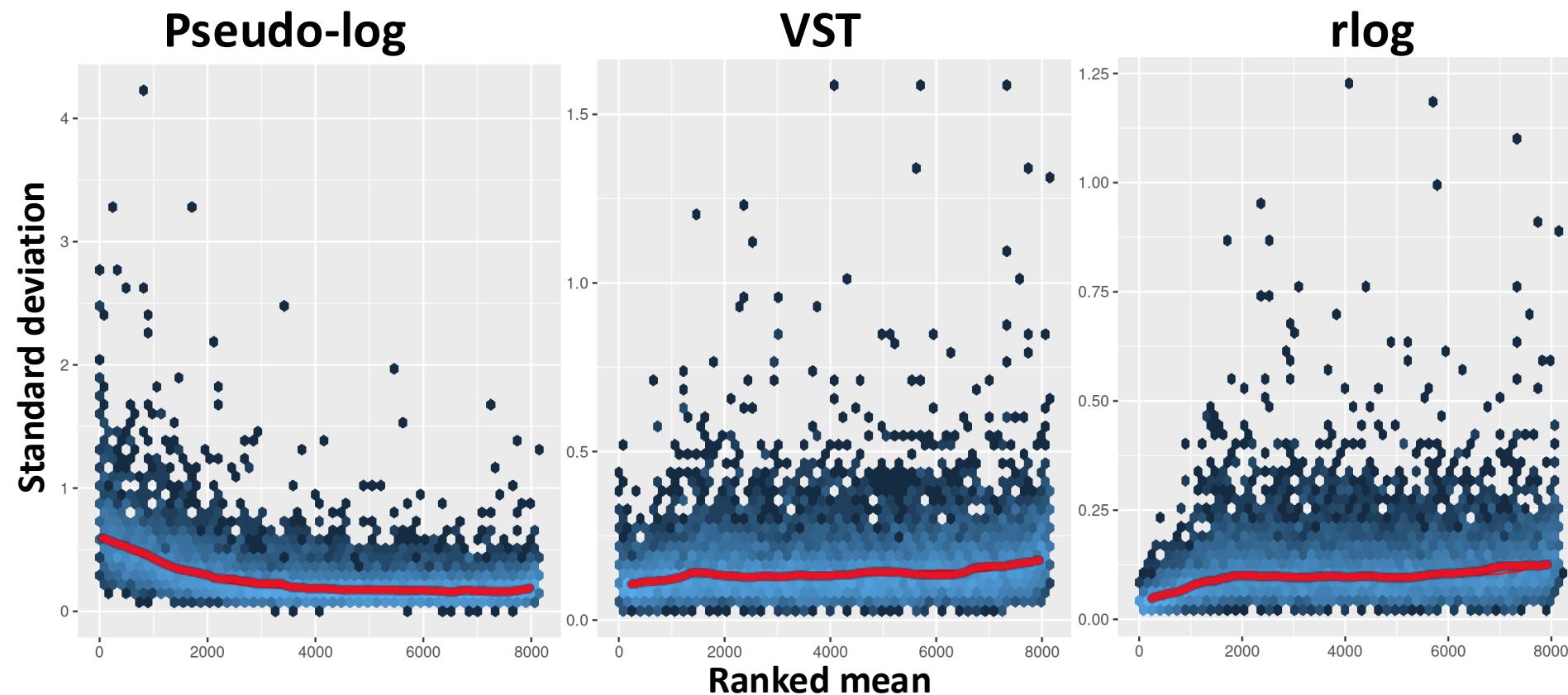
- Pseudo-log:  $y = \log_2(n + n_0)$ 
  - $n_0$  is a constant, like 1
  - Variance not stable at low values (does not scale with expression)
- Instead, we want to transform the data to remove the trend (variances roughly similar across mean values)
- Variance stabilizing transformation *DESeq2::vst()*
- Regularized log transformation *DESeq2::rlog()*

Huber et al. 2003 Stat. Appl. Genet. Mol. Biol.,

Anders & Huber 2010 Nature,

Love et al. 2023 “Analyzing RNA-seq data with DESeq2”

# Effect of transformations on variance



# Today's lab: *Polygonia c-album*



# Orientation to the tutorial

## 2 Our questions

1 Our system: diet plasticity in generalist butterflies

### 2 Our questions

3 Background

4 Unit 1: Exploring patterns of gene expression among samples

5 Unit 2: Differential gene expression analysis

6 Unit 3: Gene set enrichment analysis

7 The big challenge: running a second contrast

8 Other great resources:

9 References

## 3 Background

Today's tutorial walks through a reference-based differential gene expression (DGE) analysis. This means our reads have been aligned to an existing reference genome for *P. c-album*, rather than a *de novo* transcriptome generated from the RNA-seq data. The three main steps of reference-based DGE analysis are 1) alignment, 2) quantification and 3) analysis (Fig. 2). In this tutorial, we will focus on **step 3) analysis**.

This tutorial has three units:

- **Exploring patterns of gene expression among samples**
- **Identifying differentially expressed genes**
- **Evaluating functional enrichment of DE gene sets**

Each unit has core exercises you should try to finish during the lab. If you finish the core exercises, there are additional challenge exercises at the end of each unit.

Occasional blue boxes give background on the analyses. Feel free to gloss over these – you can come back to them later if you are curious or want to learn more.

## 4 Unit 1: Exploring patterns of gene expression among samples

Everything in this tutorial will be done in **RStudio**.

### 4.1 Set the working directory

Open RStudio and start by checking (`getwd()`) and setting (`setwd()`) your working directory. The activity is designed to be run in the 'RNAseq\_analysis' directory.

Show

Alternatively, you can set the working directory using the RStudio interface. Click on the **Files** tab. Navigate by clicking on the directories you want to enter (`workshop_materials`, then `RNAseq_analysis`). Once inside the working directory, use the **More** drop-down menu (next to the little blue gear) and select **Set As Working Directory**.

Take a look at the contents of the directory and subdirectory. You can do this using the `list.files()` command with the `recursive = T` option, or by selecting **Go To Working Directory** from the **More** drop-down menu on the **Files** tab.

# Exploring patterns in RNAseq data

## Part 1

### Core tasks:

- Load raw count matrix
- Transform for visualization
- PCA of samples
- Hierarchical clustering of samples

### Challenge exercises

# Open work time (25 min)

Five more minutes!

5 minutes

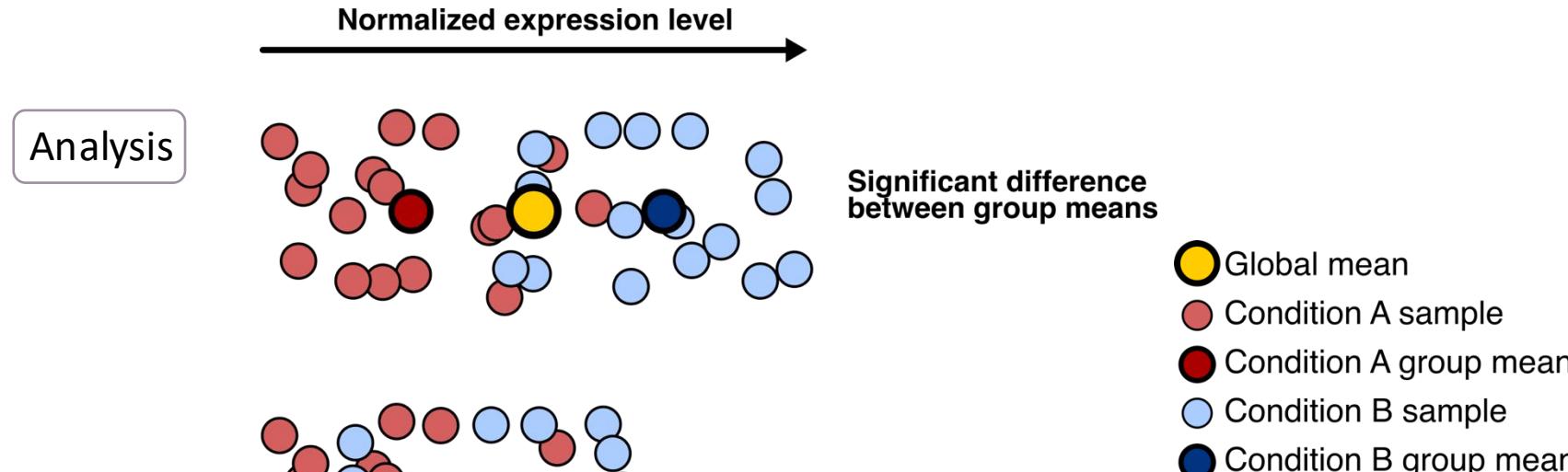


# Review

# Lab activities

- Exploring patterns in RNAseq data
- Differential gene expression analysis
- Functional enrichment of gene sets

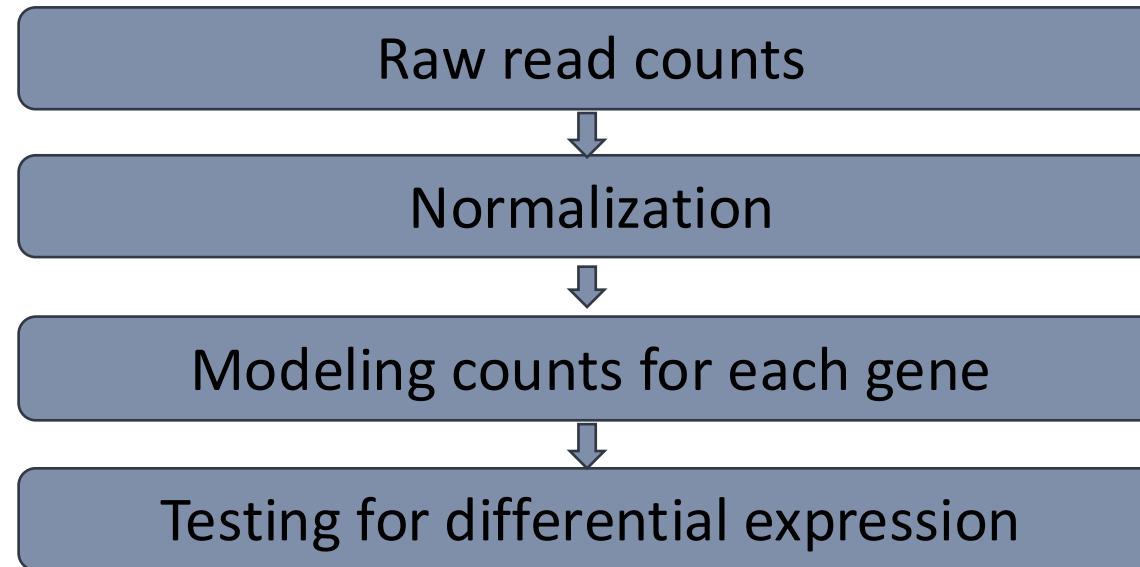
# Differential expression analysis



Input

features (e.g. genes)	samples					
Gene_id	S1	S2	S3	S4	S5	S6
Polcal_g1	17	10	5	23	10	6
Polcal_g2	0	1	0	1	2	1
Polcal_g3	7	0	2	7	4	0
Polcal_g4	17	11	5	21	10	12

# Differential expression analysis



# DESeq2 package

METHOD | [Open Access](#) | Published: 05 December 2014

## Moderated estimation of fold change and dispersion for RNA-seq data with DESeq2

[Michael I Love](#), [Wolfgang Huber](#) & [Simon Anders](#) 

[Genome Biology](#) 15, Article number: 550 (2014) | [Cite this article](#)

450k Accesses | 34853 Citations | 131 Altmetric | [Metrics](#)

# Modeling raw counts for each gene

Step 1. Normalization (aka estimation of size factors)

→ done!

Step 2. Estimate gene-wise dispersion

To accurately model sequencing counts, we need to generate accurate estimates of within-group variation for each gene (aka **dispersion**)

- need to choose the right distribution

# Statistical modeling of count data

**Which probability distributions are suitable for modeling count data?**

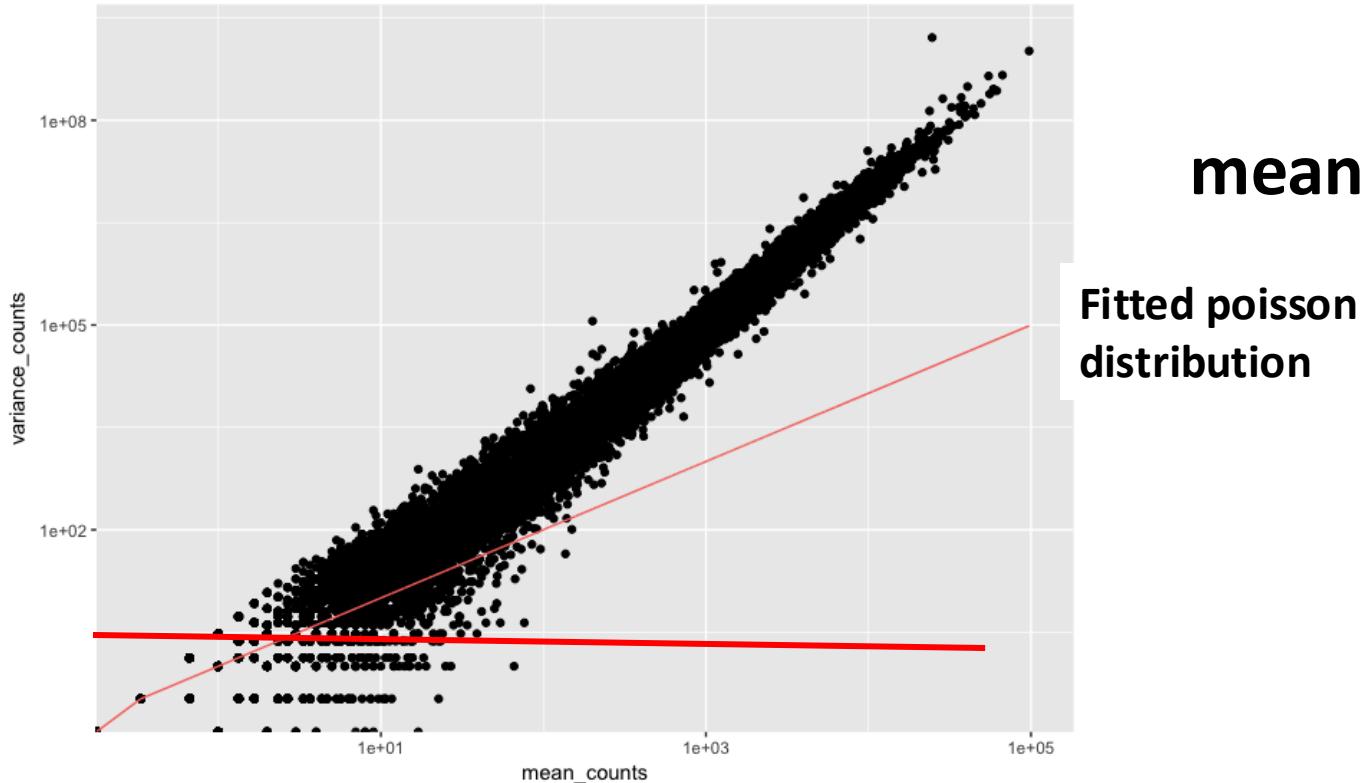
Poisson distribution?

A property of Poission distribution is that the **mean = variance**.

# Statistical modeling of count data

**Which probability distributions are suitable for modeling count data?**

Poisson distribution?

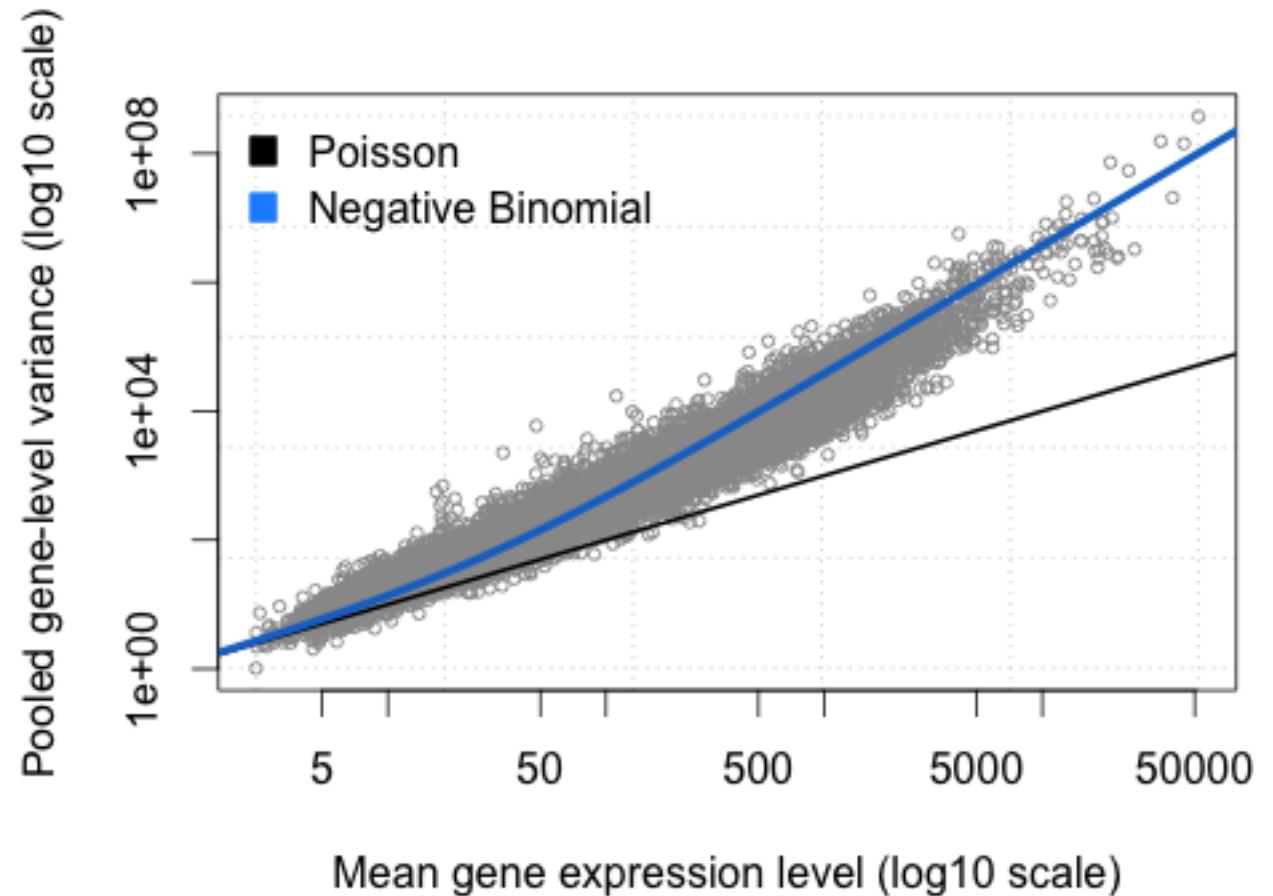


**Poisson distribution is not suitable to model count data across the biological samples.**

# Statistical modeling of count data

The distribution that fits best is the **Negative Binomial (NB)**.

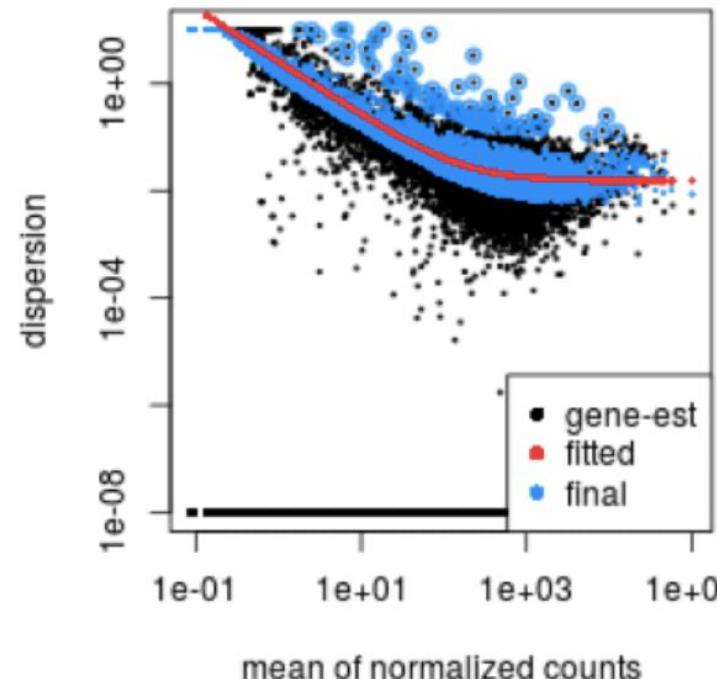
- two parameters, one for the mean and one for the variance
- flexibility to estimate the amount of **dispersion** for each gene across samples.



# How does the dispersion relate to our model?

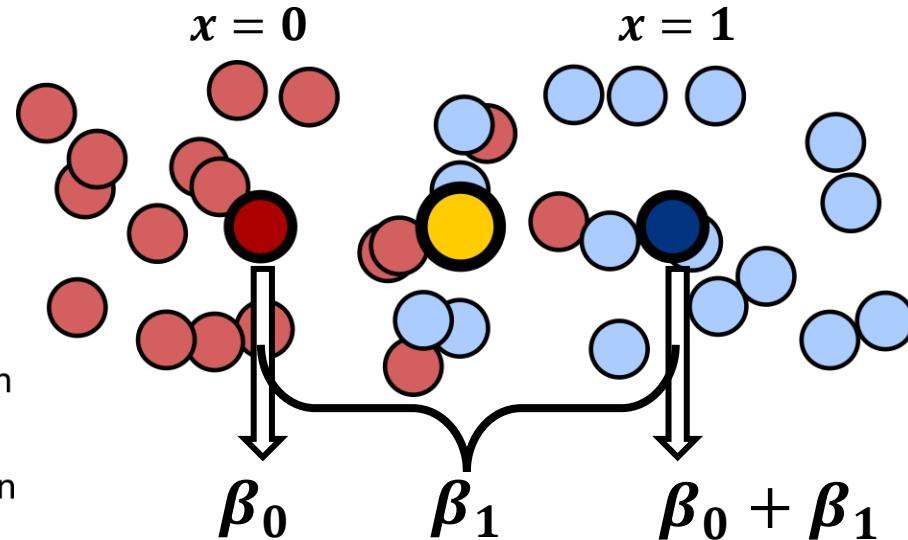
- Variation is an important part of model fitting and hypothesis testing.
- Estimates of variation for individual genes are often unreliable.
- Tools like DESeq2 share information across genes to generate more accurate estimates of variation:

**Fitted dispersion curve =  
expected dispersion for genes  
of a given level of expression  
(e.g., mean normalized count)**



# Model fitting and hypothesis testing

- Global mean
- Condition A sample
- Condition A group mean
- Condition B sample
- Condition B group mean



## Step 4. Generalized Linear Model fit for each gene

$$y = \beta_0 + x_1 \beta_1$$

- $y$  = normalized **expression level**
- $\beta_0$  = **intercept** (the estimated expression for the base level, condition A (**red**))
- $x_1$  = a binary indicator variable for (0 if part of the **red** group, 1 if part of the **blue** group)
- $\beta_1$  = coefficient for condition B (**blue**)
  - represents the **difference** between **red** and **blue**

$$y = \beta_0 + 0 * \beta_1$$

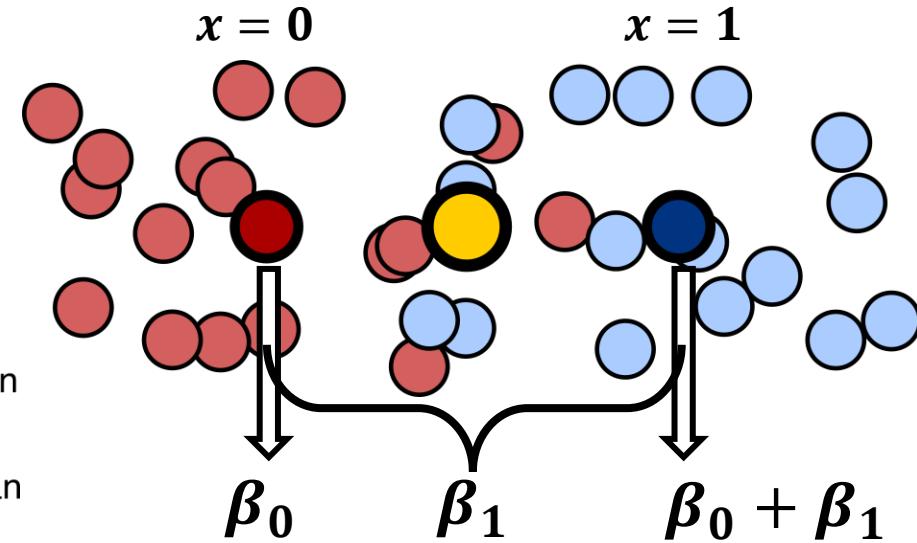
$$y = \beta_0$$

$$y = \beta_0 + 1 * \beta_1$$

$$y = \beta_0 + \beta_1$$

# Model fitting and hypothesis testing

- Global mean
- Condition A sample
- Condition A group mean
- Condition B sample
- Condition B group mean



## Step 4. Generalized Linear Model fit for each gene

$$y = \beta_0 + \beta_1$$

$$y - \beta_0 = \beta_1$$

$$\log_2(\text{expression}_{\text{blue}}) - \log_2(\text{expression}_{\text{red}}) = \beta_1$$

$$\log_2 \left( \frac{\text{expression}_{\text{blue}}}{\text{expression}_{\text{red}}} \right) = \beta_1 \text{ "log}_2 \text{ Fold Change"}$$

$$\begin{aligned}\log_2 1 &= 0 \\ \log_2 2 &= 1 \\ \log_2 4 &= 2\end{aligned}$$

# Specifying contrasts



```
Pca_dds <- DESeqDataSetFromMatrix(countData = Pca_counts,  
                                    colData = Pca_metadata,  
                                    design = ~ condition)
```

```
contrast_U_R <- c("condition", "Urtica", "Ribes")  
  
# extract the results for your specified contrast  
Pca_res_table_U_R <- results(Pca_dds_filt, contrast=contrast_U_R)
```

$$\log_2 \left( \frac{\text{expression}_{\text{Ribes}}}{\text{expression}_{\text{Urtica}}} \right) = \beta_1 \quad \text{"log}_2 \text{ Fold Change"}$$

# Output of DESeq2

log2 fold change (MLE): condition Urtica vs Ribes

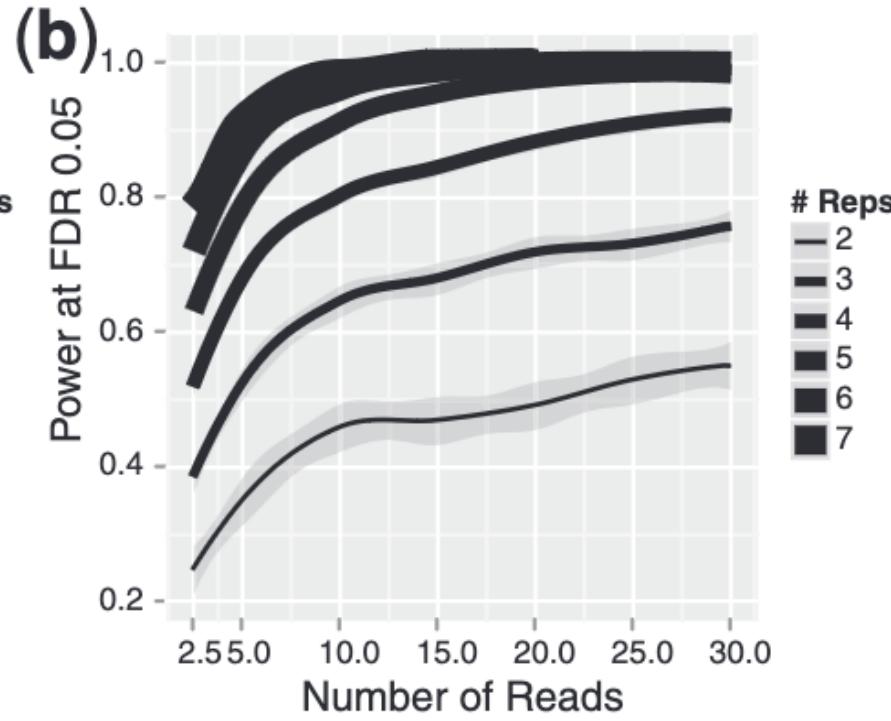
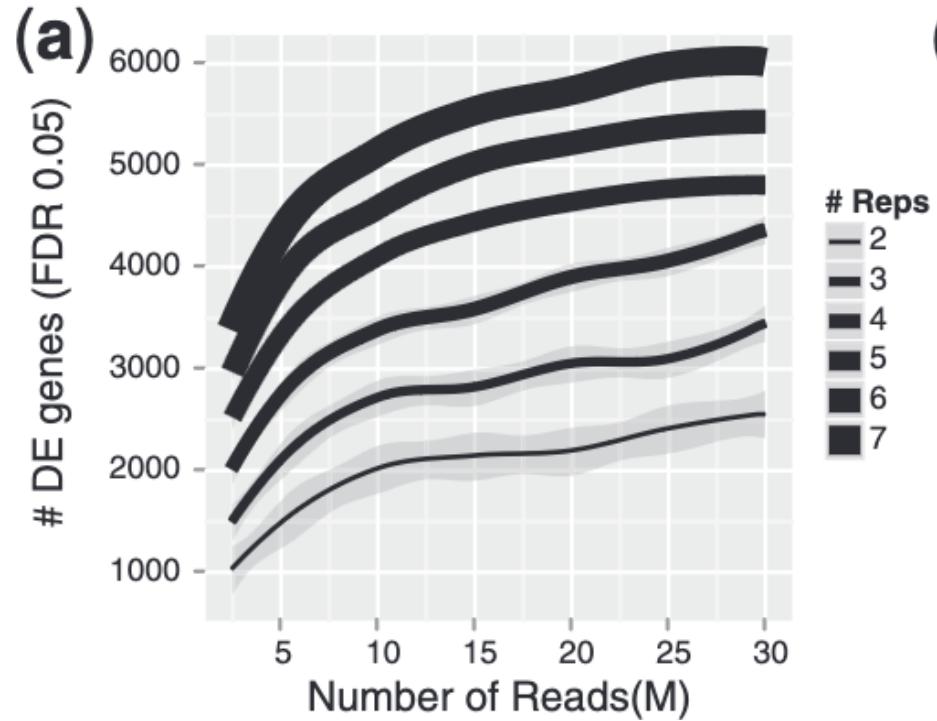
Wald test p-value: condition Urtica vs Ribes

DataFrame with 10253 rows and 6 columns

	baseMean	log2FoldChange	lfcSE	stat	pvalue	padj
	<numeric>	<numeric>	<numeric>	<numeric>	<numeric>	<numeric>
Polcal_g10	89.7562	0.2644909	0.164662	1.606262	0.108216	0.248881
Polcal_g100	128.7307	0.0751998	0.120094	0.626174	0.531201	0.702218
Polcal_g1000	80.8697	-0.0682283	0.117253	-0.581890	0.560641	0.724417
Polcal_g10000	18.4347	0.0794954	0.237090	0.335296	0.737402	0.846199
Polcal_g10006	19.1902	0.4310584	0.295618	1.458158	0.144797	0.304659
...	...	...	...	...	...	...
Polcal_g9993	15.1301	-0.181906	0.356393	-0.51041	0.6097642	0.7610362
Polcal_g9994	16.6881	0.402894	0.294354	1.36874	0.1710811	0.3409535
Polcal_g9996	84.0056	0.140555	1.025049	0.13712	0.8909358	0.9396940
Polcal_g9998	2.9282	-1.638792	0.745256	-2.19897	0.0278803	0.0941556
Polcal_g9999	4.0105	-1.006017	0.598296	-1.68147	0.0926717	0.2240950

1. baseMean: mean of normalized counts for all samples
2. log2FoldChange: log2 fold change
3. lfcSE: standard error
4. stat: Wald statistic
5. pvalue: Wald test p-value
6. padj: BH adjusted p-values – use a pre-defined cutoff for significance

# When can we detect differential expression?



Liu et al. 2014. Bioinformatics

# RNASeqPower

This is the **released** version of RNASeqPower; for the **devel** version, see [RNASeqPower](#).

## Sample size for RNAseq studies

platforms all rank 549 / 2361 support 0 / 0 in Bioc 13 years build ok updated before release dependencies 0

DOI: [10.18129/B9.bioc.RNASeqPower](https://doi.org/10.18129/B9.bioc.RNASeqPower)

```
> library(RNASeqPower)
> rnapower(depth=20, cv=.4, effect=c(1.25, 1.5, 1.75, 2),
  alpha= .05, power=c(.8, .9))
      0.8      0.9
1.25 66.204618 88.629200
1.5  20.051644 26.843463
1.75 10.526332 14.091771
2     6.861294  9.185326
```

# RNASeqPower

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DOI: [10.18129/B9.bioc.RNASeqPower](https://doi.org/10.18129/B9.bioc.RNASeqPower)

```
> rnapower(depth=8, n=10, cv=0.1, effect=c(1.5, 1.75, 2),  
alpha=.05)
```

1.5	1.75	2
0.6941394	0.9258762	0.9880395

# Additional tools for study design (or post-hoc evaluation)

- ssizerNA (2016, updated 2025)

[Home](#) > [BMC Genomics](#) > Article

## Commentary: a review of technical considerations for planning an RNA-Sequencing experiment

Review | [Open access](#) | Published: 14 October 2025

Volume 26, article number 918, (2025) | [Cite this article](#)

Article | [Open access](#) | Published: 19 November 2025

### Optimized murine sample sizes for RNA sequencing studies revealed from large scale comparative analysis

[Gabor Halasz](#), [Jennifer Schmahl](#), [Nicole Negron](#), [Min Ni](#), [Wei Keat Lim](#), [Gurinder S. Atwal](#), [Yu Bai](#) & [David J. Glass](#) 

[Nature Communications](#) **16**, Article number: 10173 (2025) | [Cite this article](#)

9489 Accesses | 1 Citations | 102 Altmetric | [Metrics](#)

# What do we do with DE genes?

- Visualize expression levels,  $\log_2$  fold changes, and significance
- Identify up- and down-regulated genes
- Compare sets of DE genes
- Test for functional enrichment of DE gene sets

# Differential gene expression

- Part 2 Core tasks:
  - Run a pairwise contrast
  - Visualize differential expression with a volcano plot
  - Extract the list of DE genes
  - Visualize DE genes in a heatmap
- Challenge exercises
- Challenge questions

# Open work time

Five more minutes!

5 minutes



# Review

# Part 3: Functional enrichment

Differential expression or clustering analysis can produce large gene sets.

How can we figure out the functional consequences of these differences?

Gene set enrichment analysis:

Do functional terms occur in the target gene set more than expected by chance?

GO terms

KEGG pathways

Reactome pathways

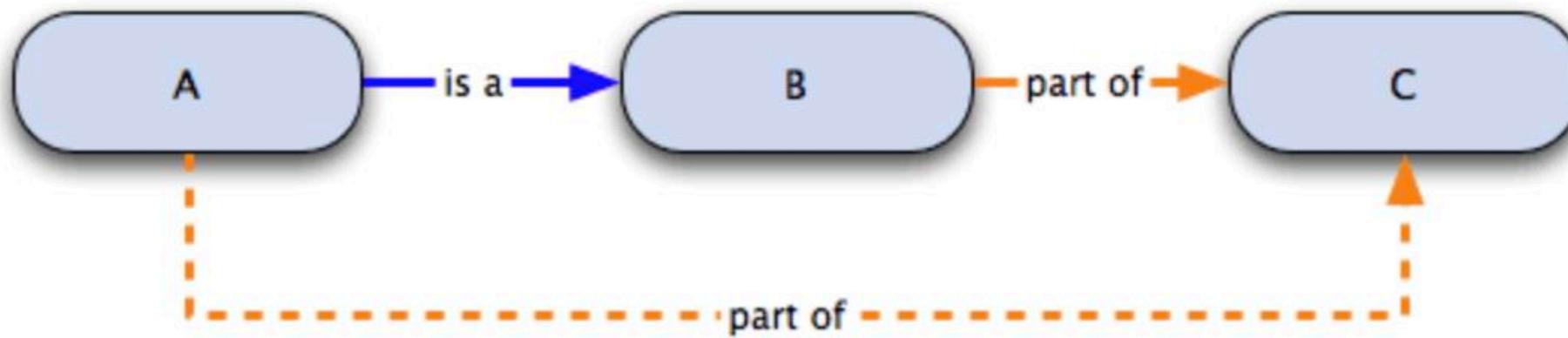
# GO term enrichment

*background frequency:* 
$$\frac{\text{genes annotated with the GO term in full annotation}}{\text{total genes in full annotation}}$$

*sample frequency:* 
$$\frac{\text{genes annotated with GO term in sample}}{\text{total genes in sample}}$$

**P-value** is the probability or chance of seeing the sample frequency, given the background frequency.

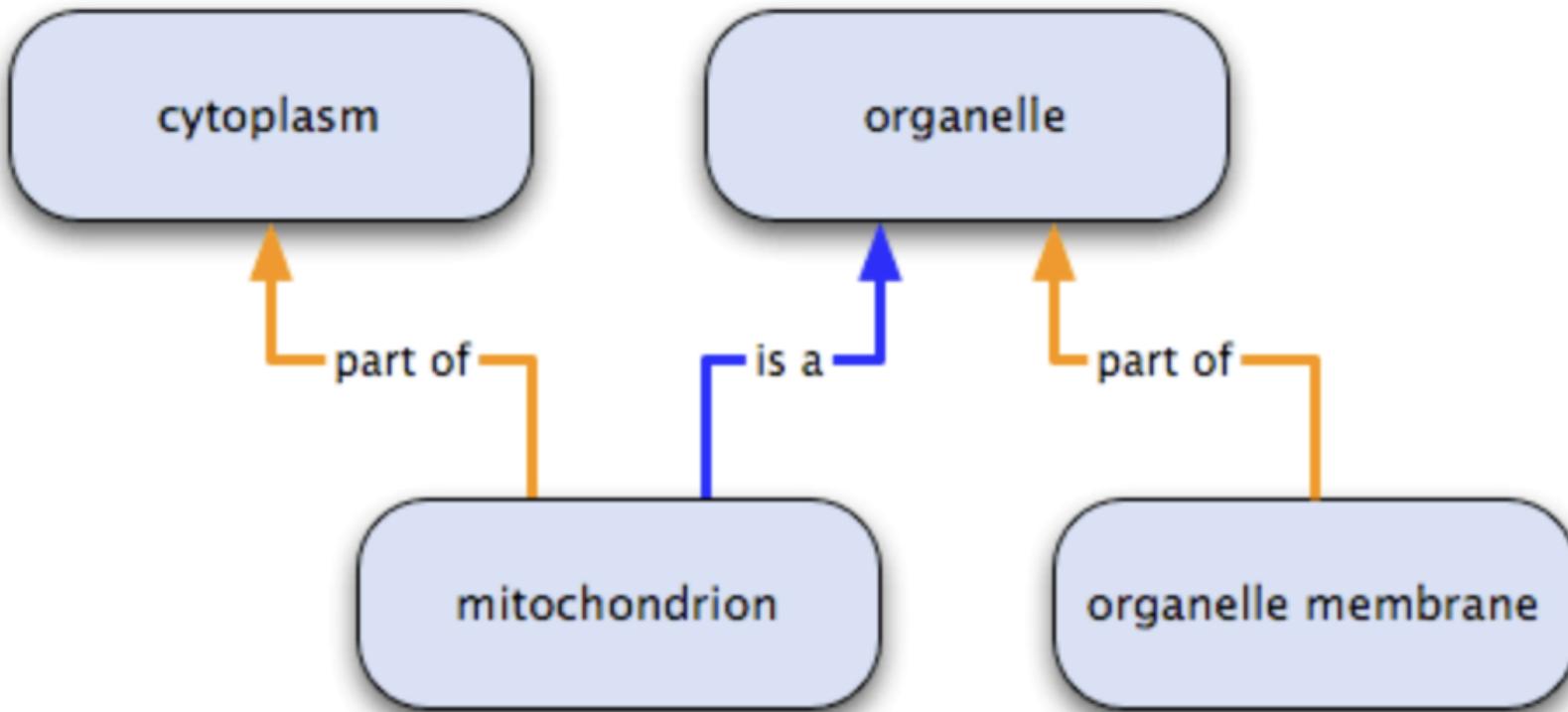
# GO relations



**Relations in the Gene Ontology**

<https://geneontology.org/docs/ontology-relationships/>

# GO relations



**Relations in the Gene Ontology**

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# Links to other DE/DS tools

Tool	Use	Link to best resource
<b>WGCNA (R package)</b>	Weighted gene coexpression analysis groups genes into modules/clusters by expression patterns across samples	Tutorial: <a href="https://fuzzyatelin.github.io/bioanth-stats/module-F21-Group1/module-F21-Group1.html#Weighted_Gene_Correlation_Network_Analysis">https://fuzzyatelin.github.io/bioanth-stats/module-F21-Group1/module-F21-Group1.html#Weighted_Gene_Correlation_Network_Analysis</a>
<b>DEXSeq (R package)</b>	Differential exon expression within the DESeq2 framework from exon count data	Vignette: <a href="https://bioconductor.org/packages/release/bioc/vignettes/DEXSeq/inst/doc/DEXSeq.html">https://bioconductor.org/packages/release/bioc/vignettes/DEXSeq/inst/doc/DEXSeq.html</a>
<b>EdgeR (R package)</b>	Differential expression analysis with differential exon expression functions from exon count data Good when: few reps, lowly expressed genes	User guide: <a href="https://bioconductor.org/packages/release/bioc/vignettes/edgeR/inst/doc/edgeRUsersGuide.pdf">https://bioconductor.org/packages/release/bioc/vignettes/edgeR/inst/doc/edgeRUsersGuide.pdf</a>
<b>Limma (R package)</b>	Differential expression analysis with complex experimental designs, including batch and random effects	Vignette: <a href="https://www.bioconductor.org/packages/release/bioc/vignettes/limma/inst/doc/intro.html">https://www.bioconductor.org/packages/release/bioc/vignettes/limma/inst/doc/intro.html</a>
<b>LeafCutter (python &amp; R scripts)</b>	Differential splicing analysis specifically focused on differential intron retention from junction count data	Github page: <a href="https://davidaknowles.github.io/leafcutter/">https://davidaknowles.github.io/leafcutter/</a>
<b>IsoformSwitchAnalyzer (R package)</b>	Differential isoform usage from transcript count data	Vignette: <a href="https://bioconductor.org/packages/release/bioc/vignettes/IsoformSwitchAnalyzer/inst/doc/IsoformSwitchAnalyzer.html">https://bioconductor.org/packages/release/bioc/vignettes/IsoformSwitchAnalyzer/inst/doc/IsoformSwitchAnalyzer.html</a>
<b>EBSeq</b> 2026-01-21	Bayesian differential expression framework	Vignette: <a href="https://bioconductor.org/packages/release/bioc/vignettes/EBSeq/inst/doc/EBSeq_Vignette.pdf">https://bioconductor.org/packages/release/bioc/vignettes/EBSeq/inst/doc/EBSeq_Vignette.pdf</a> Github page: <a href="https://github.com/lengning/EBSeq">https://github.com/lengning/EBSeq</a>

# Median of ratios (MRN) normalization

- Used by DESeq2 (DGE analysis tool we will use today)

Let's see how the normalization works...

### Step 1. Create a pseudo-reference sample for each gene (row-wise geometric mean)

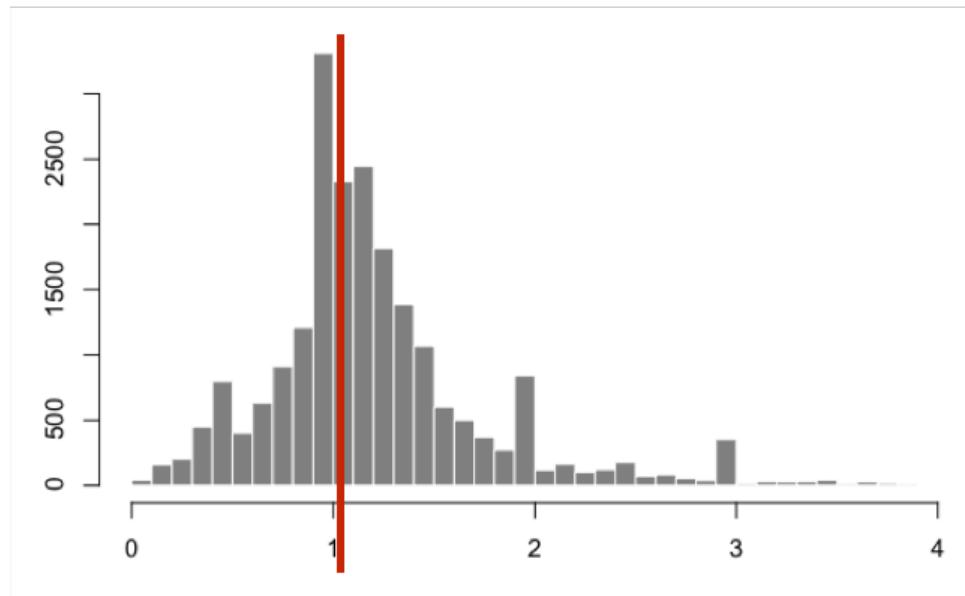
Gene	sampleA	sampleB	Pseudo-reference sample
EF2A	1489	906	$\sqrt{1489*906} = 1161.5$
ABCD1	22	13	$\sqrt{22*13} = 16.9$
...	...	...	...

### Step 2. Calculates ratio of each sample to the reference

Gene	sampleA	sampleB	Pseudo-reference sample	Ratio of sampleA/ref	Ratio of sampleB/ref
EF2A	1489	906	1161.5	$1489/1161.5 = 1.28$	$906/1161.5 = 0.78$
ABCD1	22	13	16.9	$22/16.9 = 1.30$	$13/16.9 = 0.77$
MEFV	793	410	570.2	$793/570.2 = 1.39$	$410/570.2 = 0.72$
...	...	...	...	...	...

The figure below illustrates the median value for the distribution of all gene ratios for a single sample (frequency is on the y-axis).

sample 1 / pseudo-reference sample



The median of ratio methods makes the assumption that not ALL genes are differentially expressed; therefore, the normalization factors should account for sequencing depth and RNA composition of the sample (large outlier genes will not represent the median ratio values).

### Step 3. Calculate the normalization factor for each sample (size factor)

Gene	sampleA	sampleB	Pseudo-reference sample	Ratio of sampleA/ref	Ratio of sampleB/ref
EF2A	1489	906	1161.5	$1489/1161.5 = 1.28$	$906/1161.5 = 0.78$
ABCD1	22	13	16.9	$22/16.9 = 1.30$	$13/16.9 = 0.77$
MEFV	793	410	570.2	$793/570.2 = 1.39$	$410/570.2 = 0.72$
...	...	...	...	...	...

```
median(c(1.28, 1.3, 1.39, 1.35, 0.59,...))  
=1.3
```

```
median(c(0.78, 0.77, 0.72, 0.8, 0.73, ...))  
=0.77
```

## Step 4: calculate the normalized count values using the normalization factor

Raw counts:

Gene	sampleA	sampleB
EF2A	1489	906
ABCD1	22	13
...	...	...

Normalized counts

Gene	sampleA	sampleB
EF2A	$1489/1.3 = 1145.39$	$906/0.77 = 1176.62$
ABCD1	$22/1.3 = 16.92$	$13/0.77 = 16.88$
...	...	...

Normalized counts are not whole numbers!