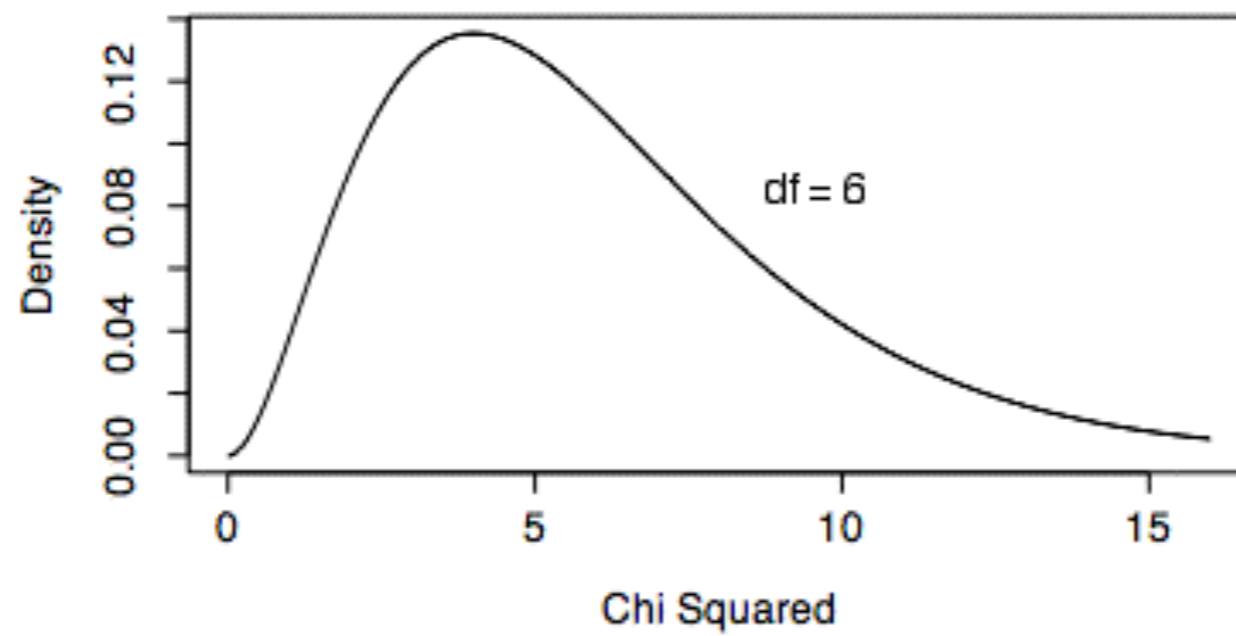
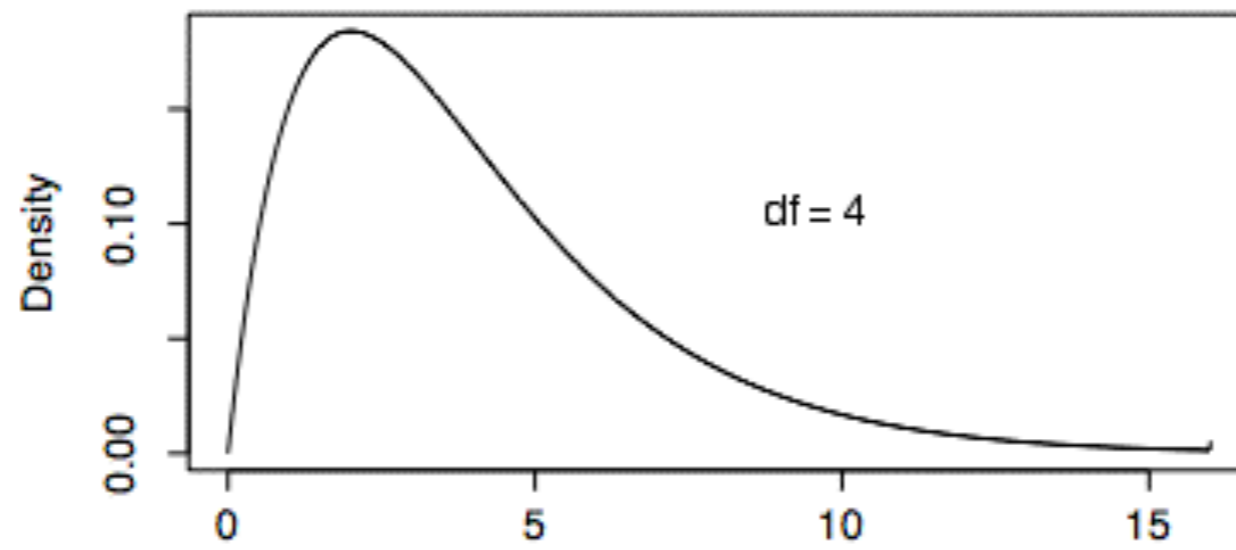
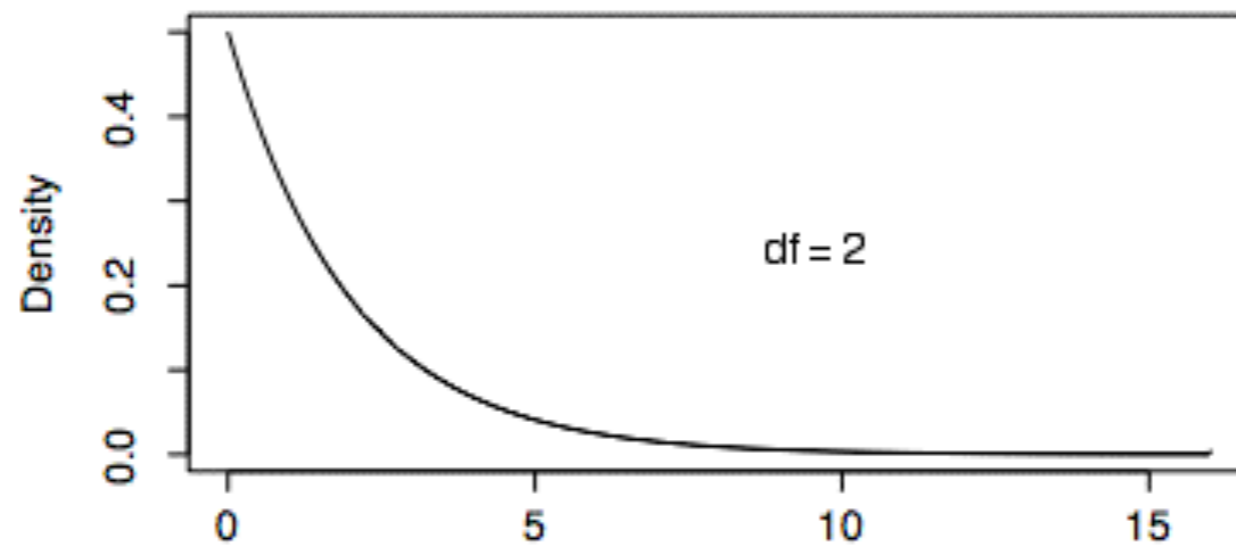
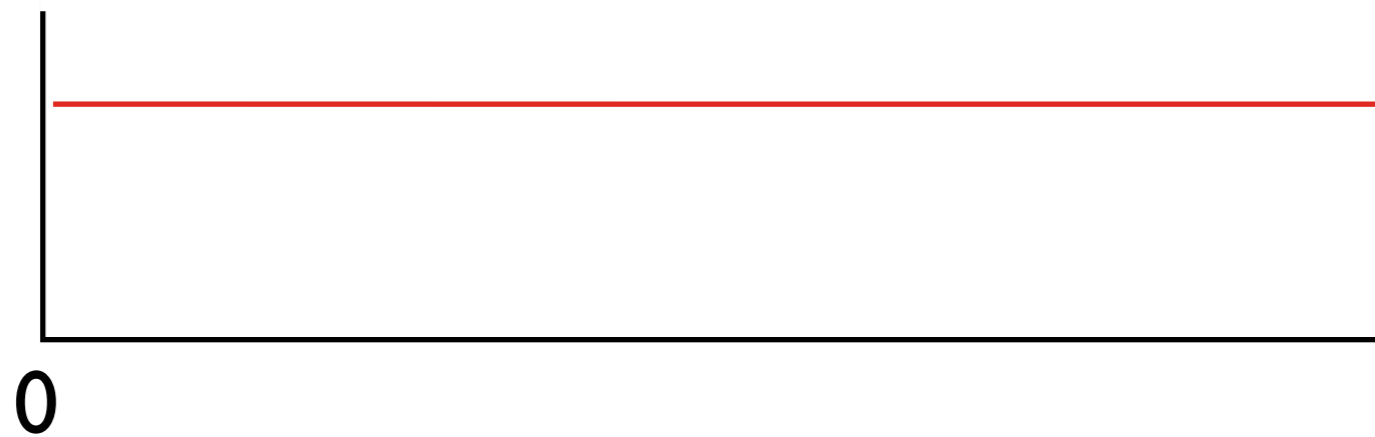


Distributions have tails.



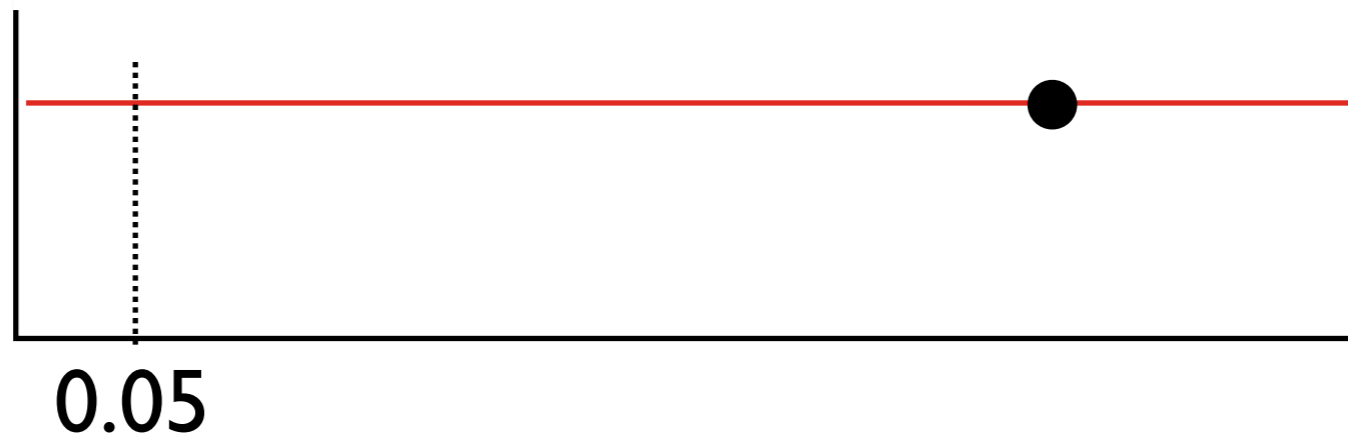
# P-values



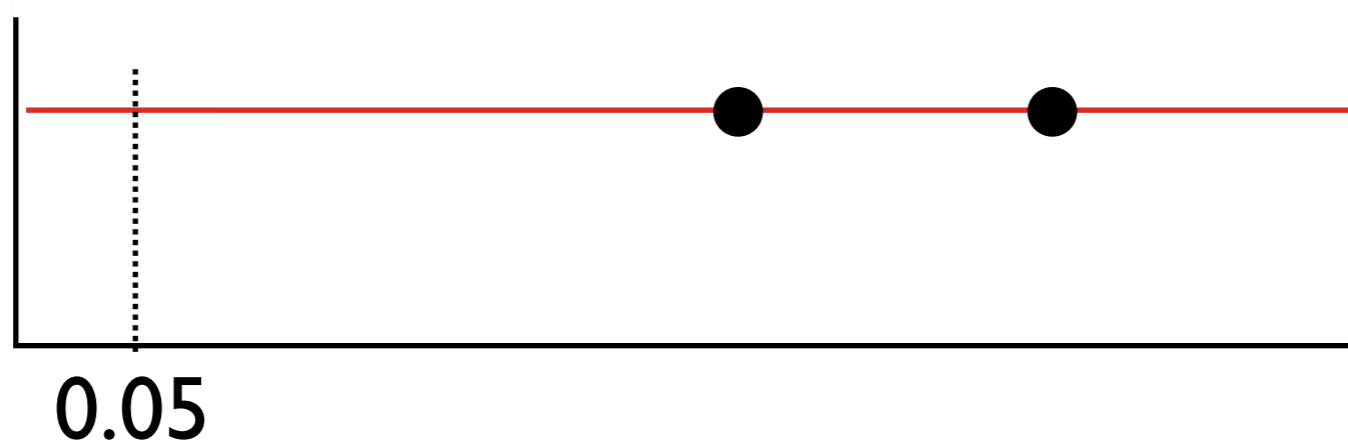
P-values are uniformly distributed under the null hypothesis

$\alpha$  = the probability of having a *single* false positive  
(type I error)

If you are conducting a single test, then  $\alpha$  is your p-value



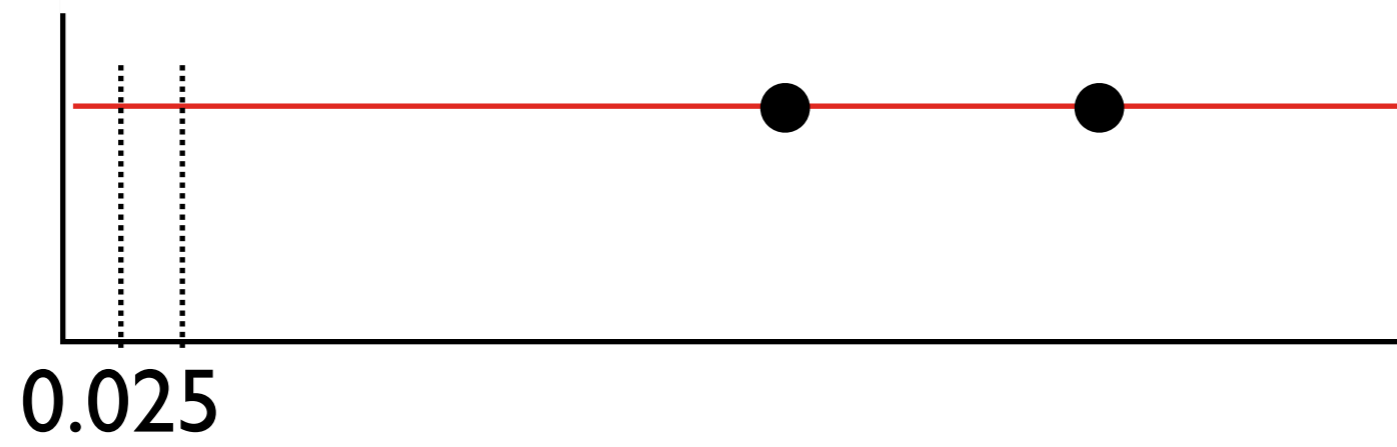
If you are conducting multiples tests, then  $\alpha$  is *not* your p-value



## Bonferroni correction

To maintain a probability,  $\alpha$ , of a single false positive, then p-value cut-off must become:

$$= \alpha/m$$



## Dunn-Sidak correction

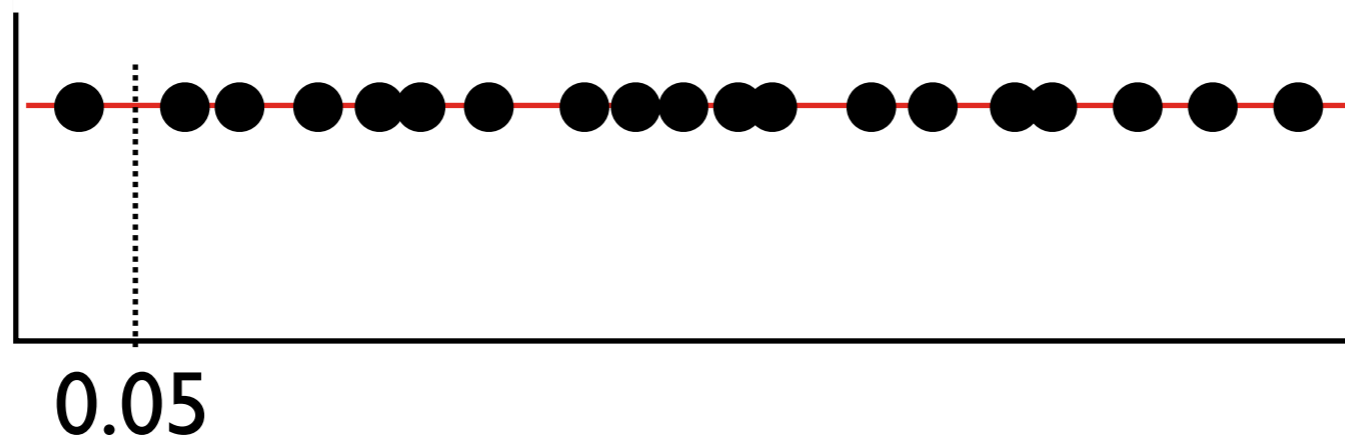
$$= 1 - (1 - \alpha)^{1/m}$$



## False Discovery Rate (FDR)

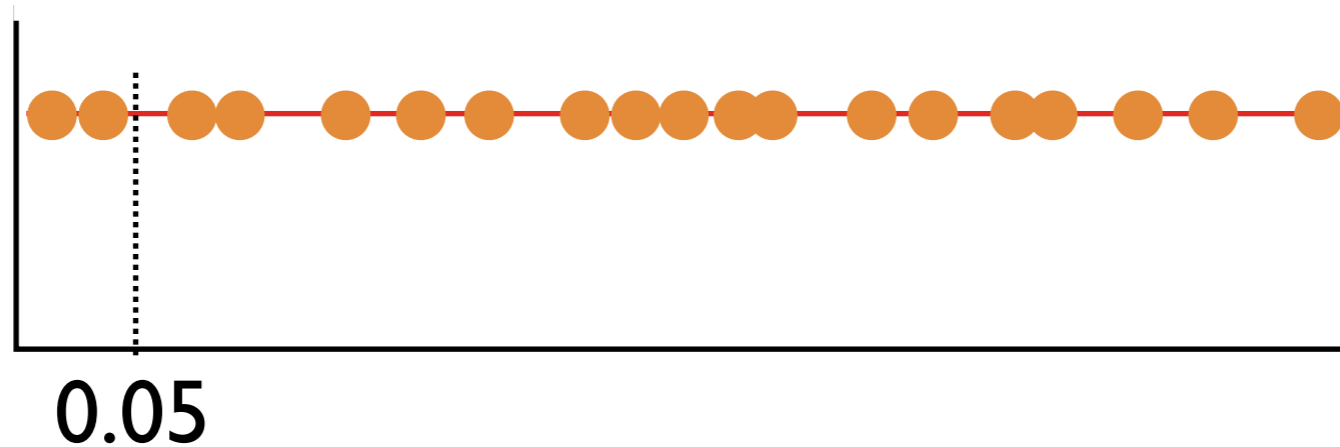
Instead of controlling probability of a single false positive, simply control fraction of false positives *among your significant tests*

## P-values



If there are no true positives, p-values are uniformly distributed

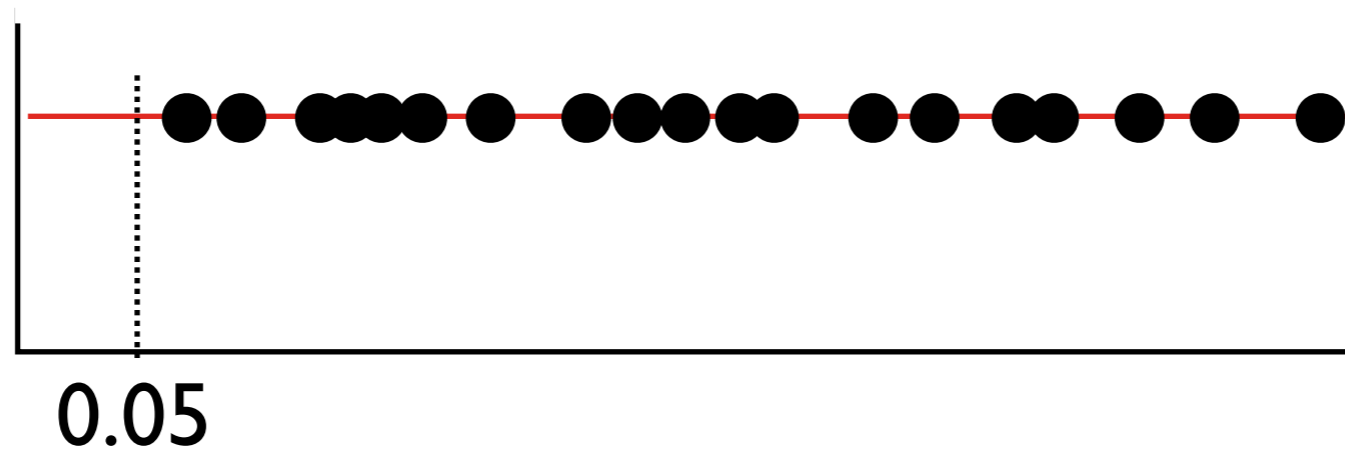
## False discovery rate



FDR = the number significant expected/  
the number significant observed

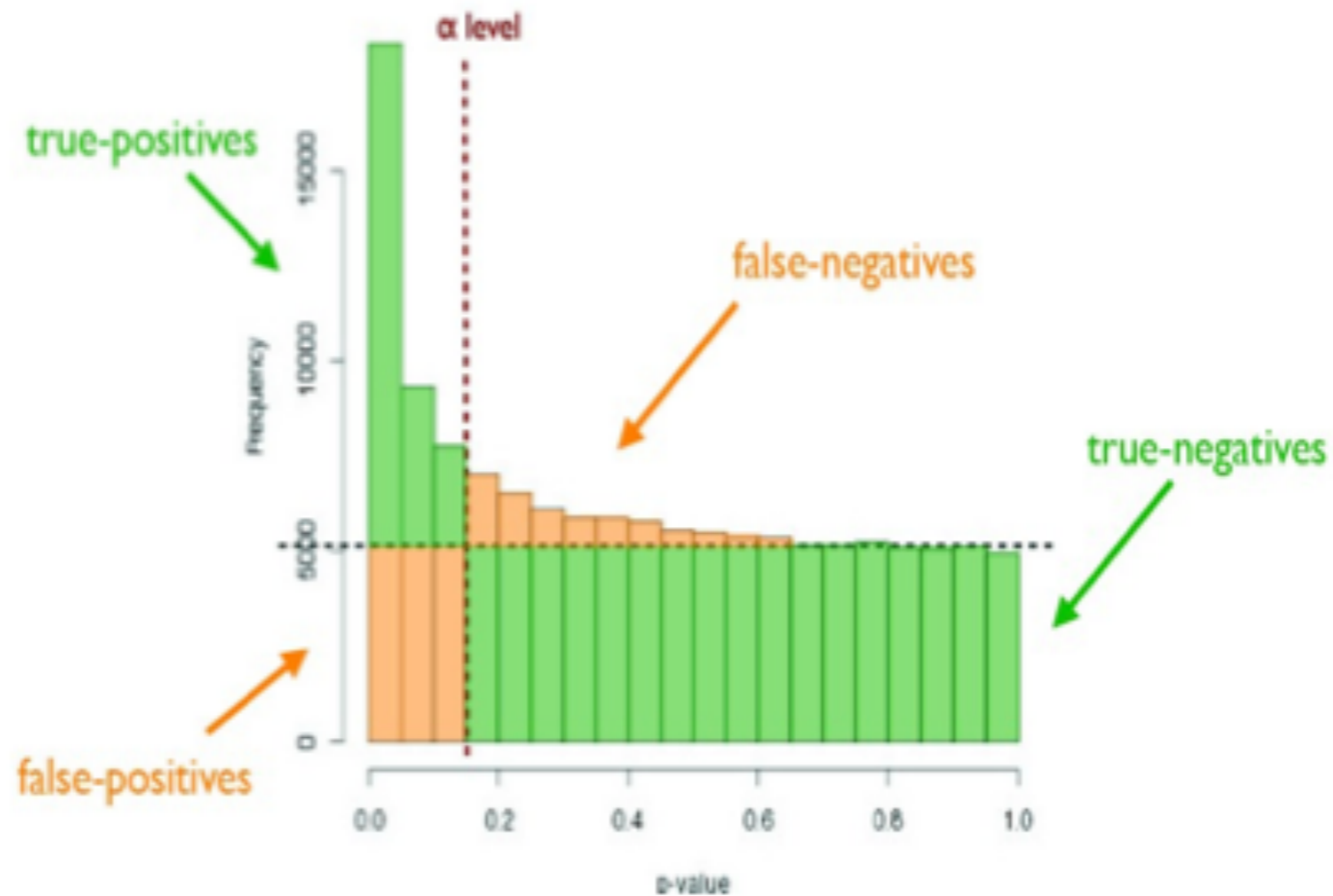
(the expected number is itself binomially distributed)

## False discovery rate



Even random data should have 5% of tests significant at 0.05

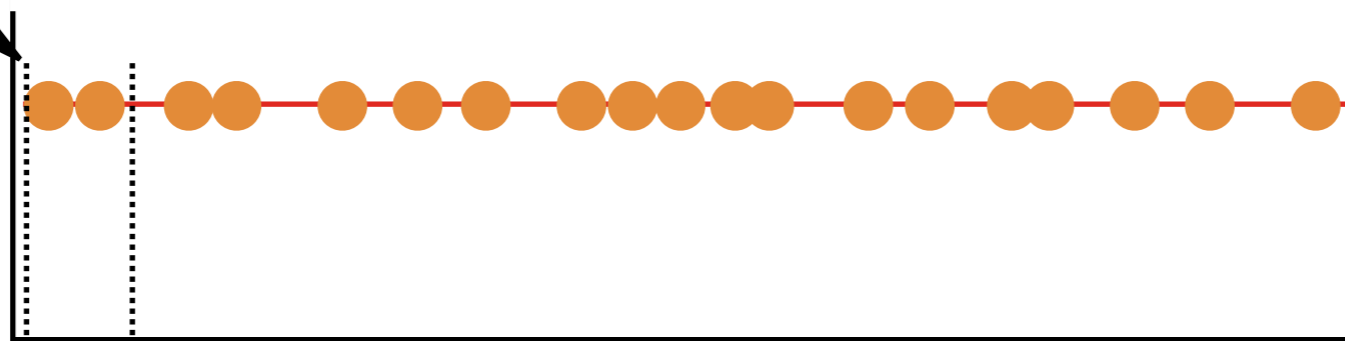
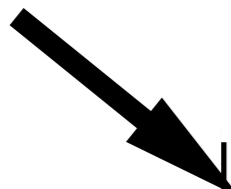
# Type I and Type II error



Real data has true positives and true negatives, as well as false positives (type I) and false negatives (type II)

# False discovery rate

0.0025



0.05

FDR helps to avoid false negatives  
(type II error)

## False Discovery Rate

$$\text{FDR} = \frac{p(i)*m}{i}$$

where  $p(i)$  is the p-value of the  $i$ th test, and  $i$  is the rank of this test in the whole list

m=100

	P-value	rank	FDR		
	0.0001	1	0.01		
	0.0002	2	0.01		
Bonf	0.001	3	0.033		
	0.001	4	0.025		
B-H	0.01	5	0.2		
		6			
		7			
		8			
		9			
	0.05	10	0.5		



There are many ways of testing for significance,  
and many different cut-offs used.

Your choice really depends on what you want to  
do next.